

Depth and Design

Contrasting AI and Human Understandings

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AAAI-18 Workshop on Knowledge Extraction from Games

The problem

- I come at this as a designer of games.
- I want to make good games.
 - Maybe computers can tell me how.
 - I don't want them to make them for me though, because I enjoy it!
- I am a lot less interested in how computers can beat games.
 - The knowledge to extract: "is this a good game?"
- I am also not interested in what a computer thinks is a good game.
 - My final platform is humans, not silicon.

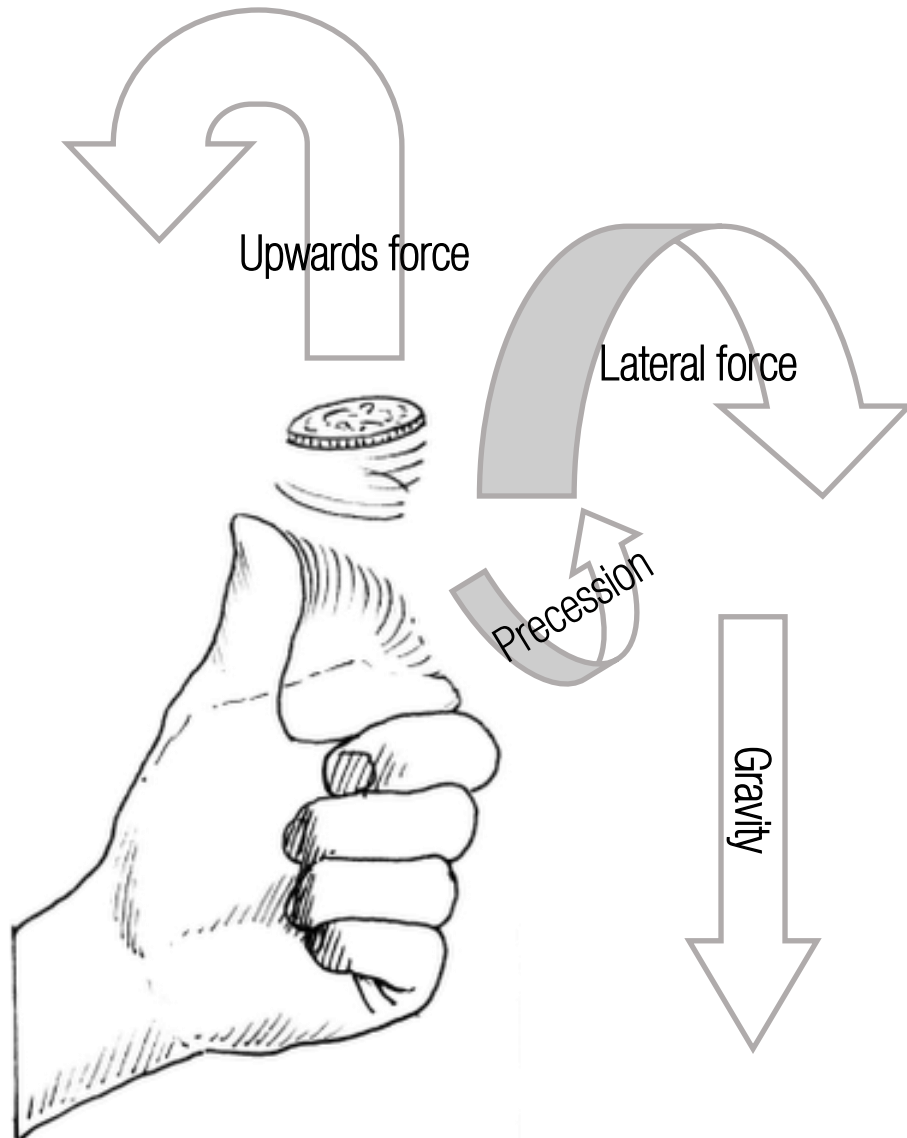
Defining “good”

- A first approximation: “fun.”
 - Best understood as a psychological **response** when we want a **quality**.
- A second approximation: “complex.”
 - There is a strong association between PSPACE-Complete (and higher) complexity class and games that audiences have termed “fun.”
 - But complex games are often not fun.
- A third approximation: “deep.”
 - There is no formal definition of “deep.”
 - It cannot mean simply large possible state space, as there are large boring games.
 - It cannot mean simply branching, as there are games with many meaningless choices.

Game grammar overview

- Games as a whole do not yet have a BNF grammar, but subdomains do.
 - Mostly used for procedural level design, for specific games.
- There is an ongoing informal project to at least identify grammatical elements.
 - Decent success here which has seeded design tooling and academic work, particularly in PCG.
- Problem: we might derive a full context-free grammar without addressing depth.
 - Fully descriptive of form, without being descriptive of scope of statements in the grammar.

A step back: the coin flip



Slight weight bias towards tails



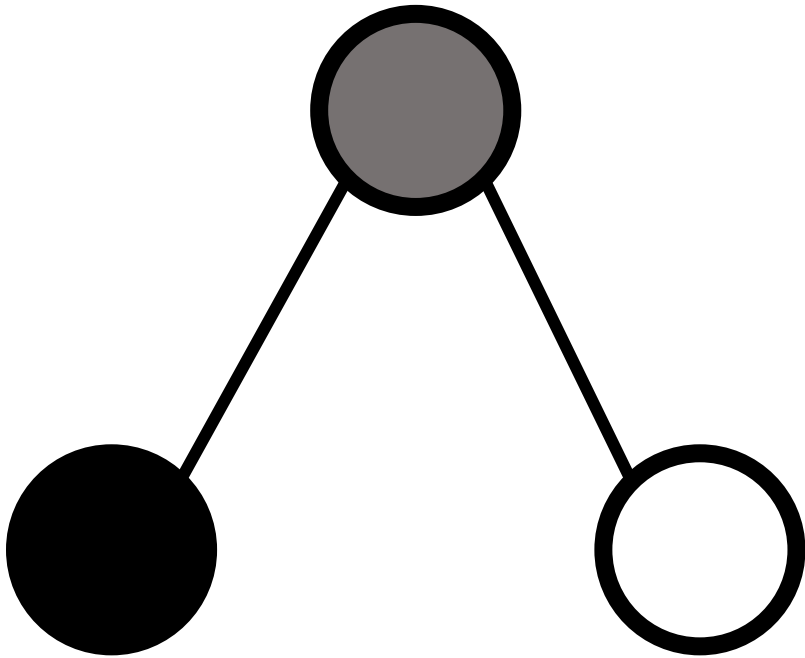
Distance to
surface

Ignored factors:

- surface elasticity
- coin elasticity
- bounces
- surface irregularity
- etc

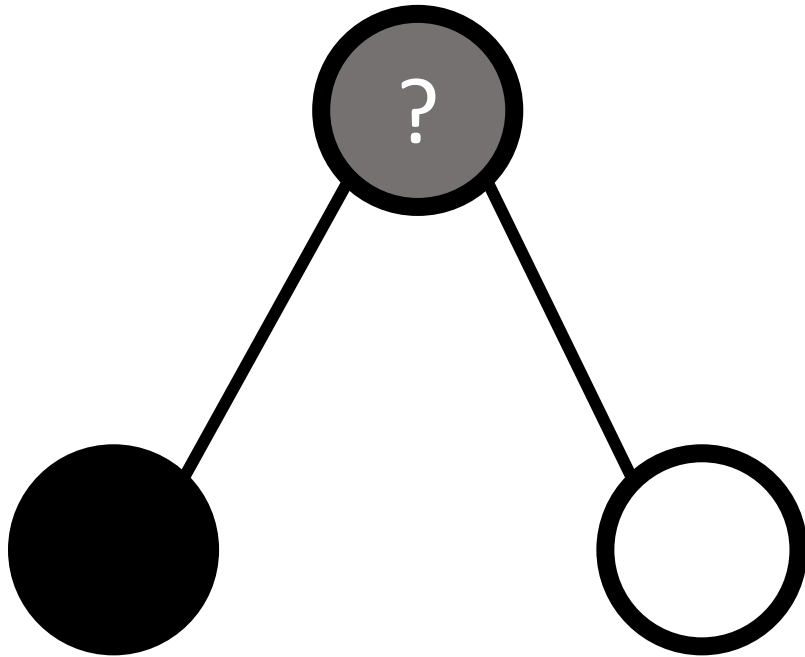


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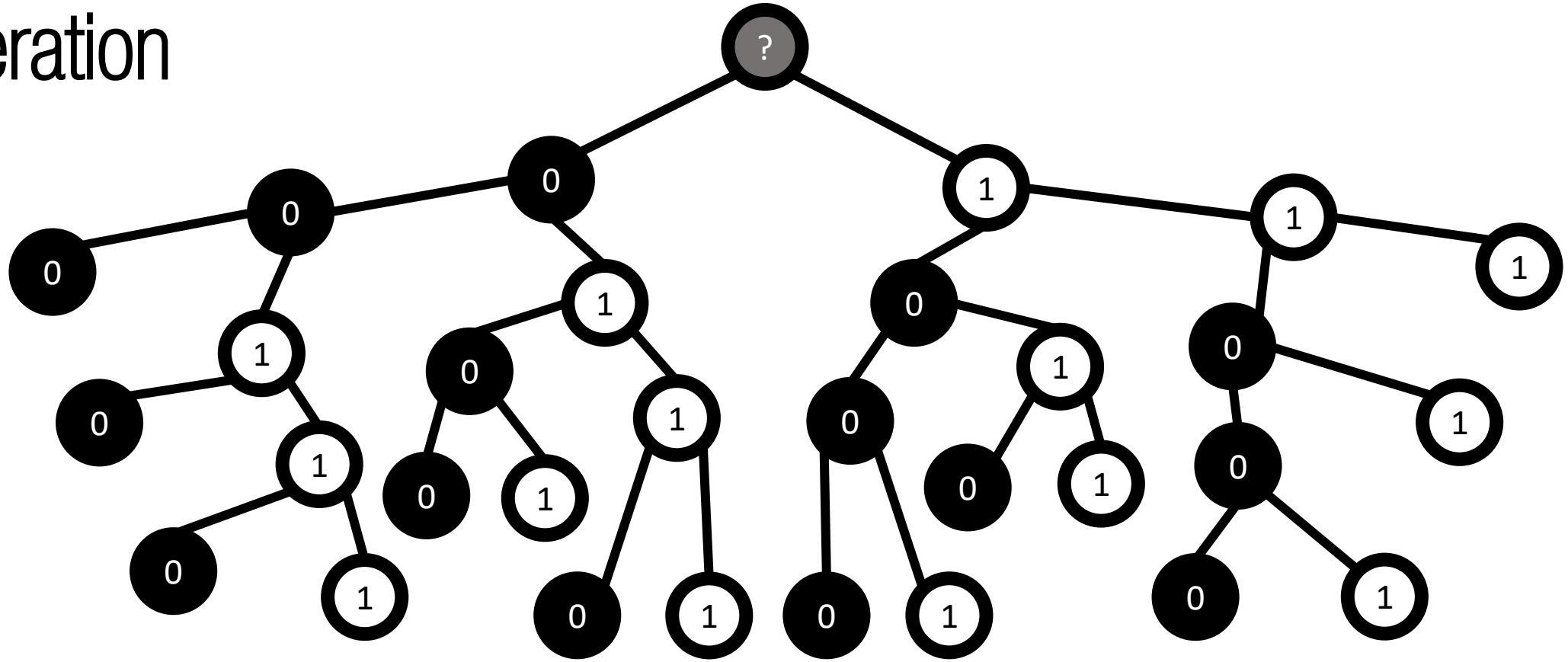
- Starts out indeterminate.
- Simple binary output.
- This is actually the case for most games.

A step back: the coin flip



- Starts out indeterminate.
- Simple binary output.
- This is actually the case for most games.
- Some end indeterminate; we call this a tie or draw.
 - (Coin bounced down the sewer...)

Iteration



- In practice simple games are played iteratively.
 - “Best of five.”
- The outcome becomes determinate at a specific point down the tree.

Forms of bounds

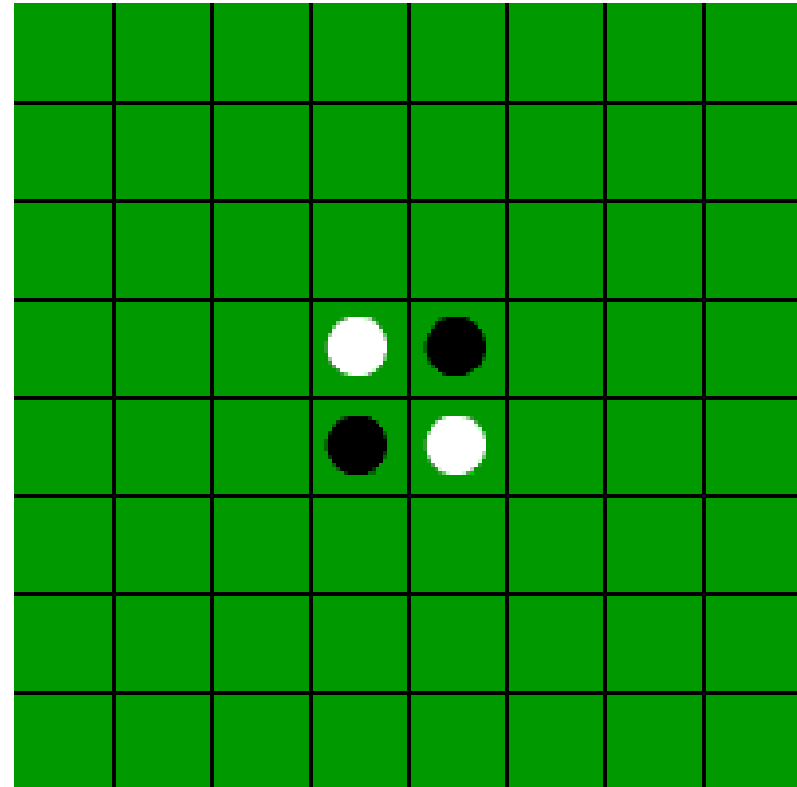
- **Goal bounded:** Reach a fixed number of points or an objective.
 - “Best of five” has a point bound of three.
 - Connect Four has a point bound of one, a singular objective.
- **Turn-bounded:** Have a higher number of victory points after a fixed set of turns.
 - Reversi has a fixed number of spaces.
 - Turns may also be token-bounded; you may have a fixed number of tokens but a choice of a larger number of spaces.

Victory points

- Term from tabletop games.
- We can generalize all those bounds into victory points.
 - Victory points in a game are not always obvious. For example, a level is a victory point in Mario.
 - Some games have multiple kinds of victory points, like Pente.
 - Score isn't usually the formal victory point in a game, but it may be the victory point in a higher-order meta-game.
- In some games victory points move in tandem with turns; in others not.
 - The parity relationship between victory points and turn/space bounds determines whether the game is binary or ternary.

Binary and ternary outcomes

- $VP_a > \text{bounds} / 2 = \text{win for black}$
- $VP_b > \text{bounds} / 2 = \text{win for white}$
- $VP_a = VP_b = \text{bounds} / 2 = \text{a draw}$
 - Possible because there's an even number of moves.

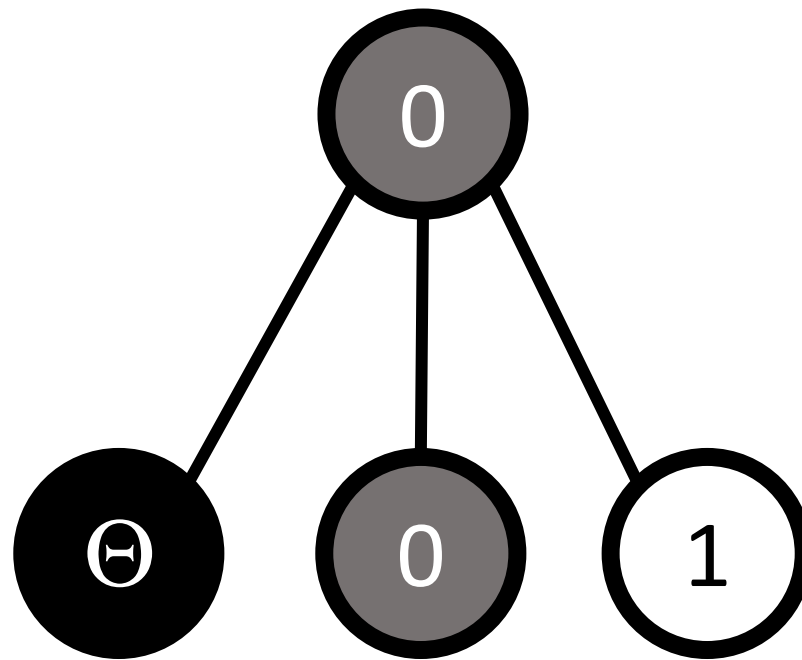


Useful game design output: three player games

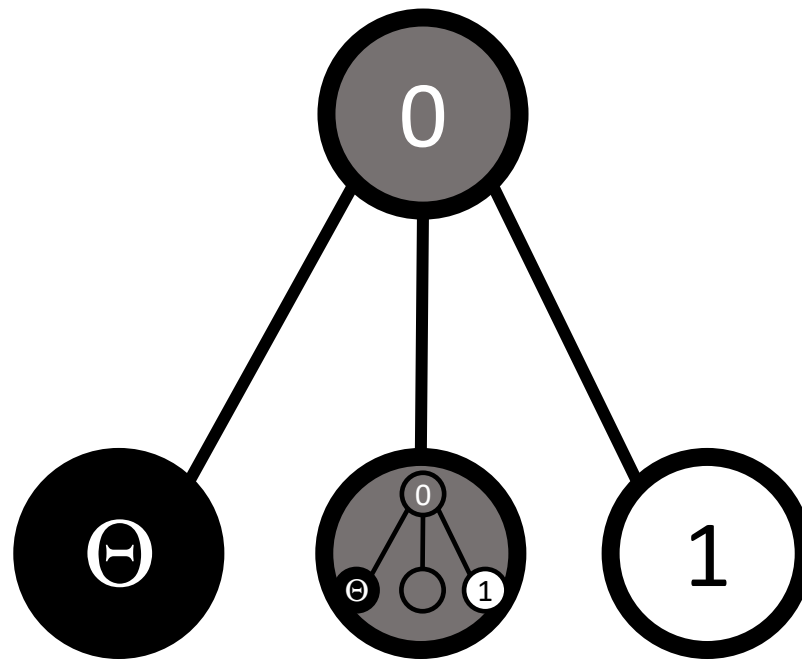
- We can generalize this to a useful design tool: $vp > \text{bound} / \text{numPlayers}$.

Number of players	Boundary	Even split		
2	64	32	ternary	<i>ties possible</i>
3	64	21.33333	binary	
3	69	23	ternary	<i>ties possible</i>
4	64	16	ternary	<i>ties possible</i>
2	65	32.5	binary	

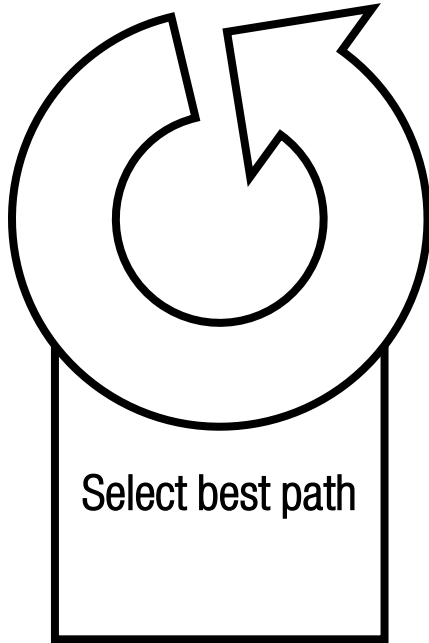
Games are generators of outcomes, distillers of processes back down to
yes,
no,
and indeterminate.



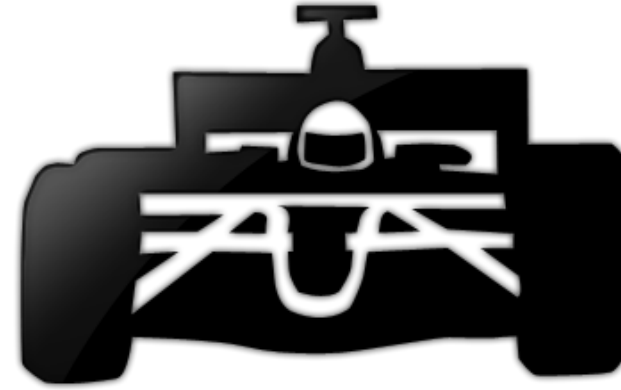
Games are also fractal,
self-similar.



An example



Cognitive
problem



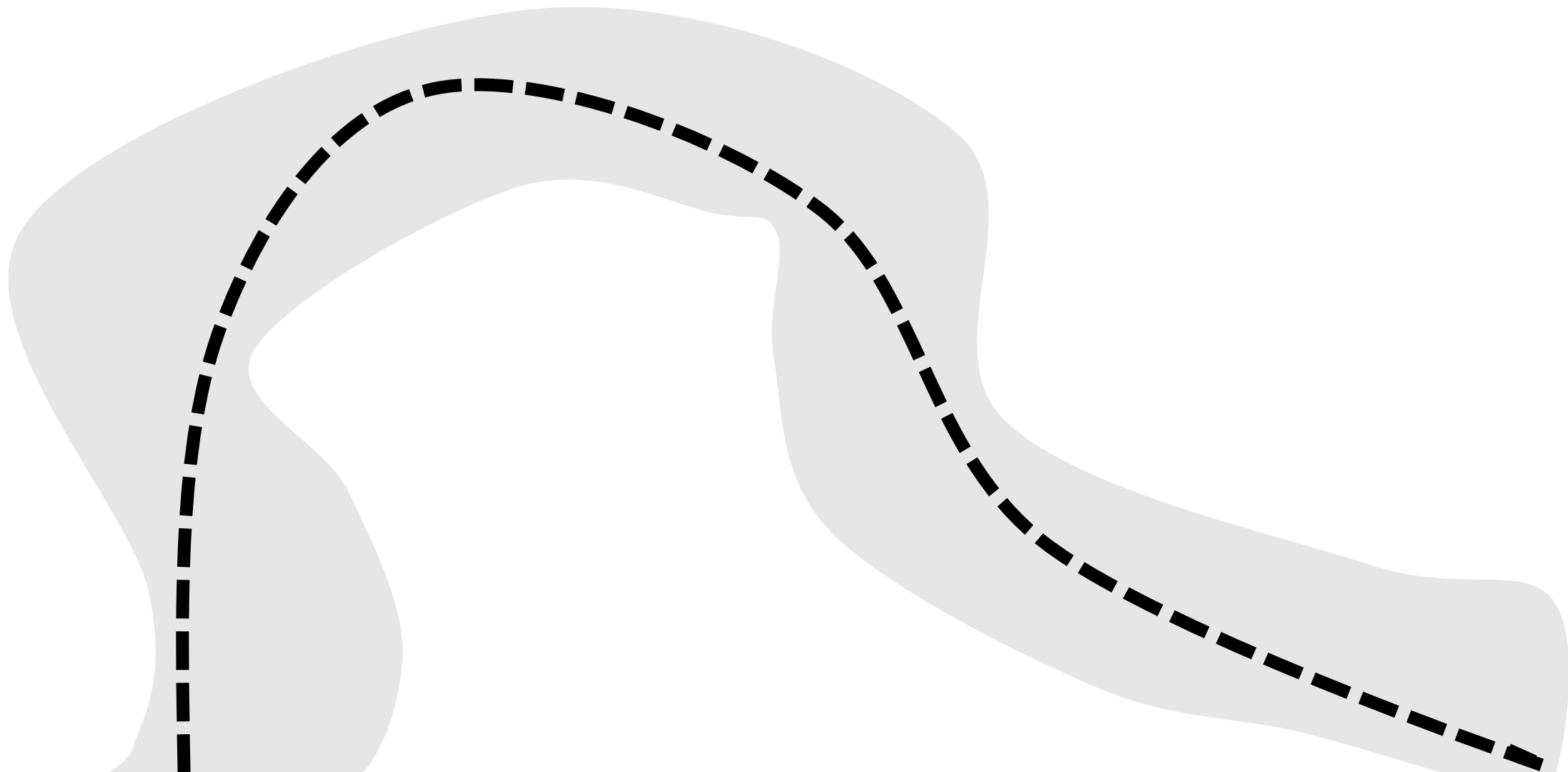
Modify for
avoidance

Steer on path

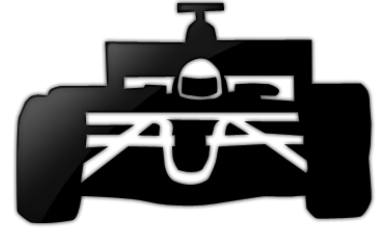
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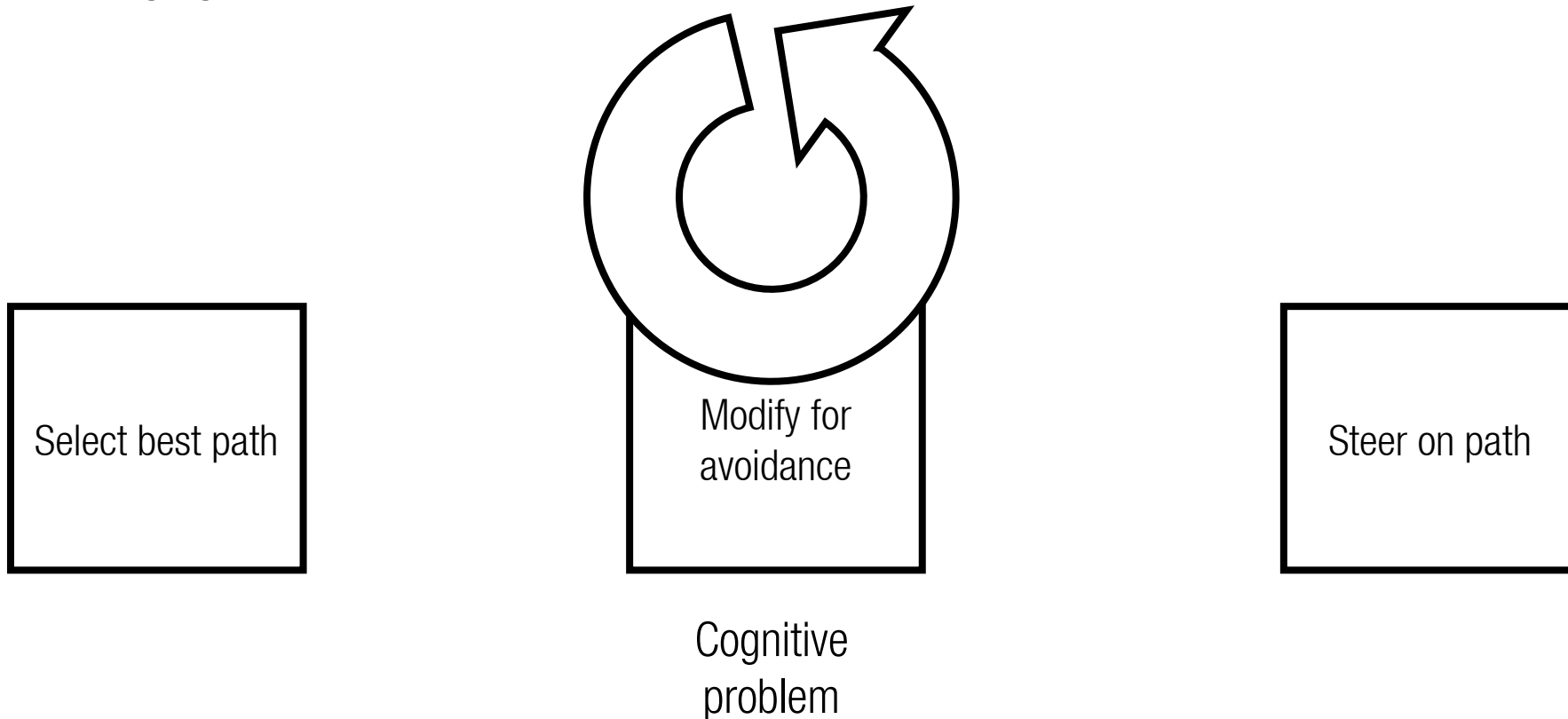
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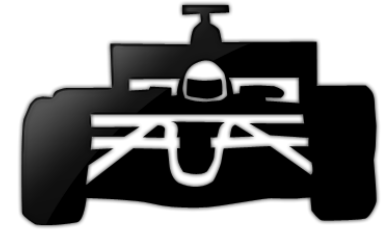
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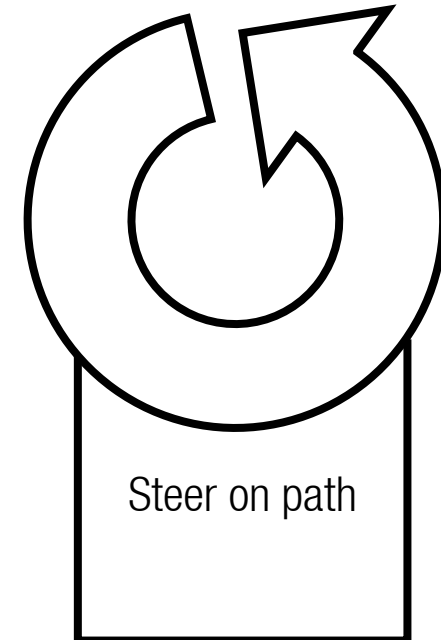
- Best possible curve path is of course constantly blocked. So at a tighter cognitive loop, you engage in avoidance.



A haptic example

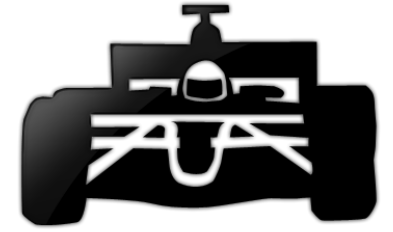


- But the tightest game loop is the loop of the controls, which is a massive autonomic and reflex challenge.

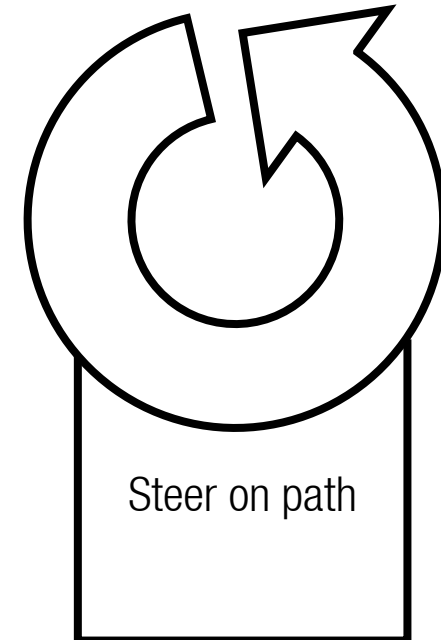
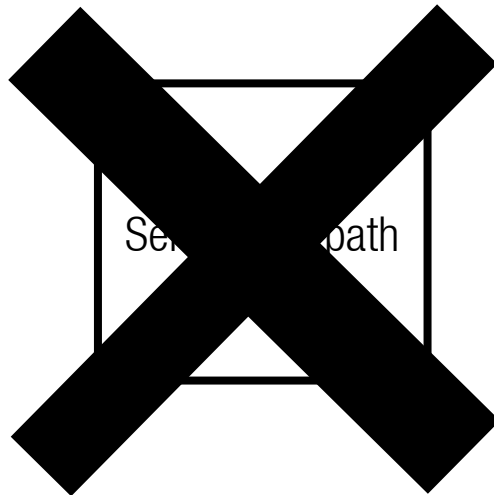


Haptic
problem

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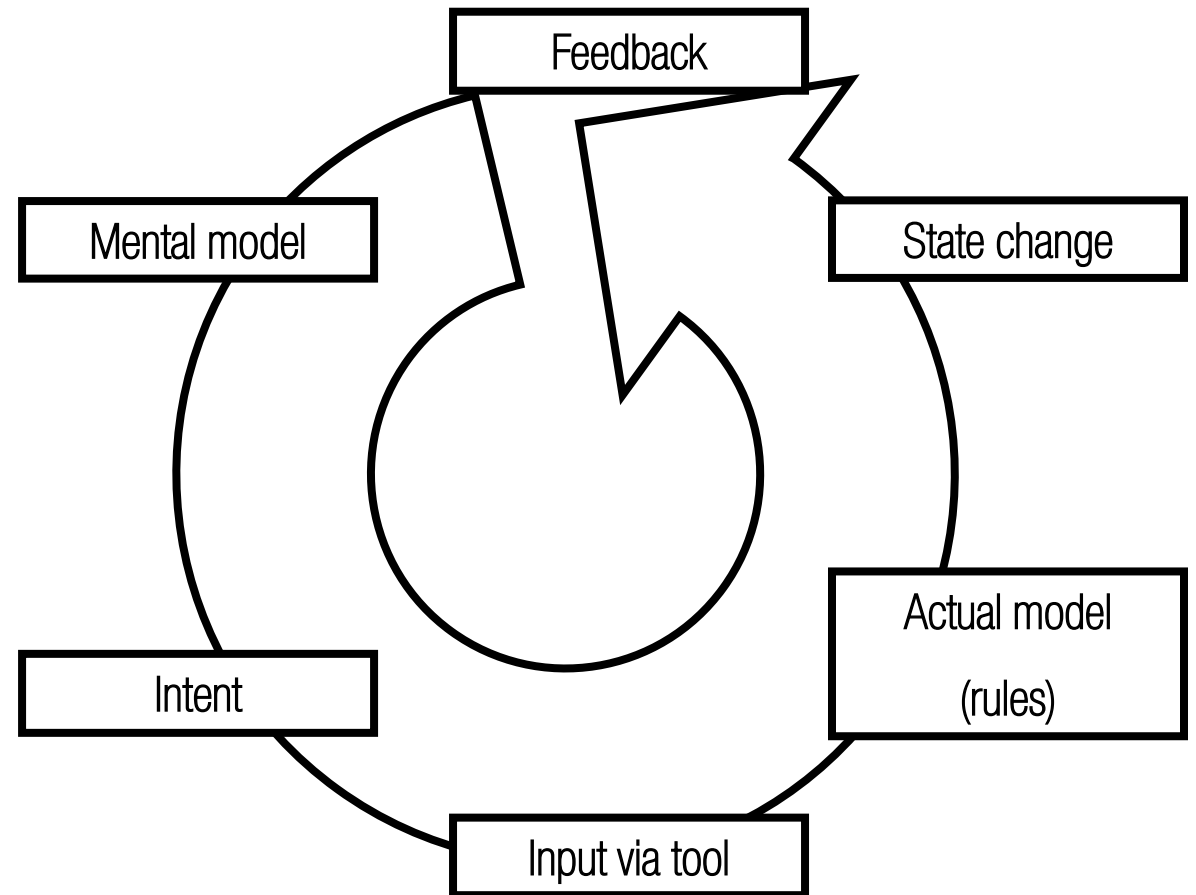


- So racing games these days **give you** the optimal path.



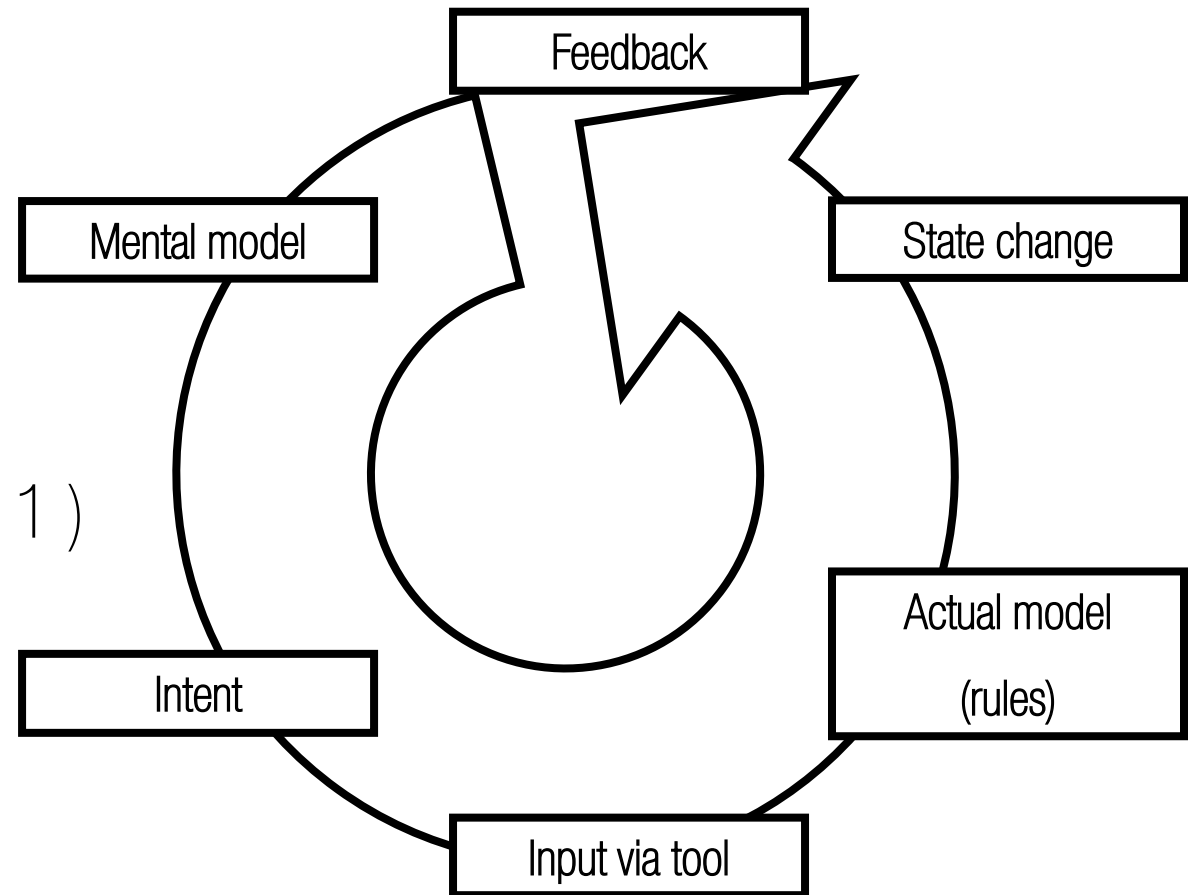
Haptic
problem

Gestures towards a BNF grammar



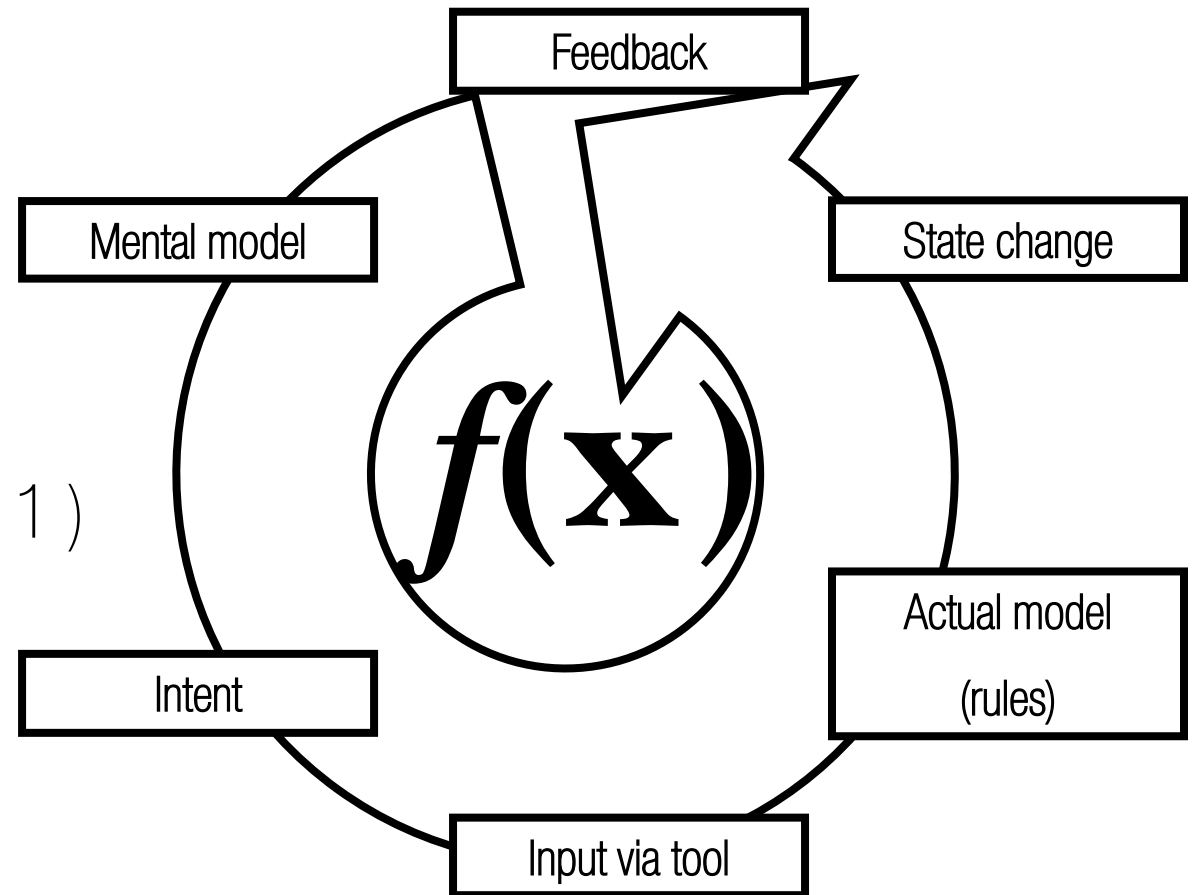
Gestures towards a BNF grammar

- $\text{game} \Rightarrow \text{game}$
- $\text{game} \Rightarrow \text{game} + \text{result}$
- $\text{result} \Rightarrow \text{system}(\text{action}) = (\Theta , [0 ,] 1)$
- $\text{result} \Rightarrow \text{system}(\text{action}) = 1$



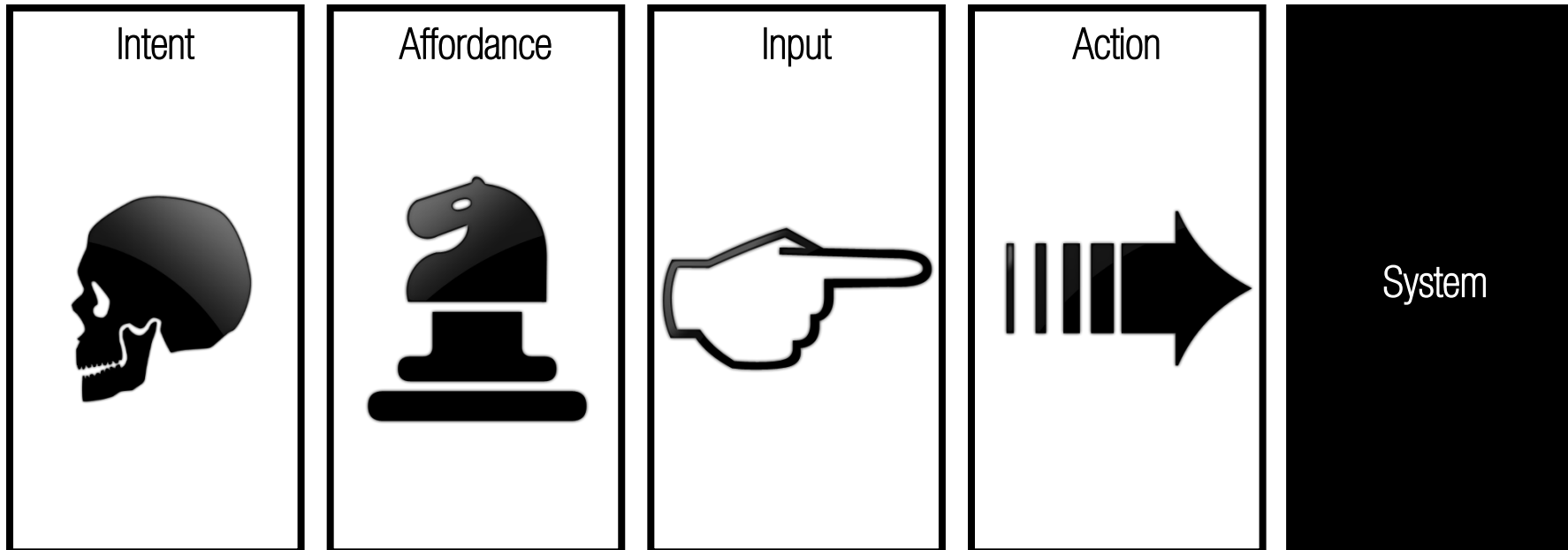
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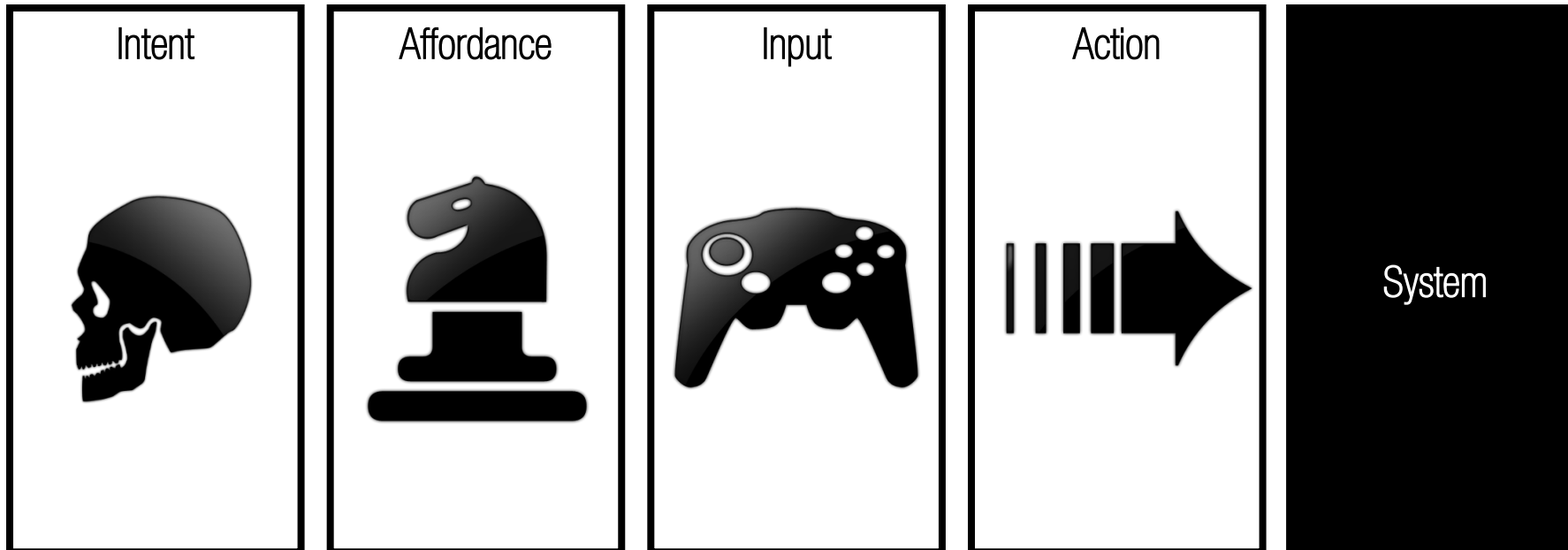
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- $\text{action} \Rightarrow \text{verb} [\{ + \text{action} \}] (\text{data})$
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- $\text{input} \Rightarrow \text{affordance} + \text{action}$



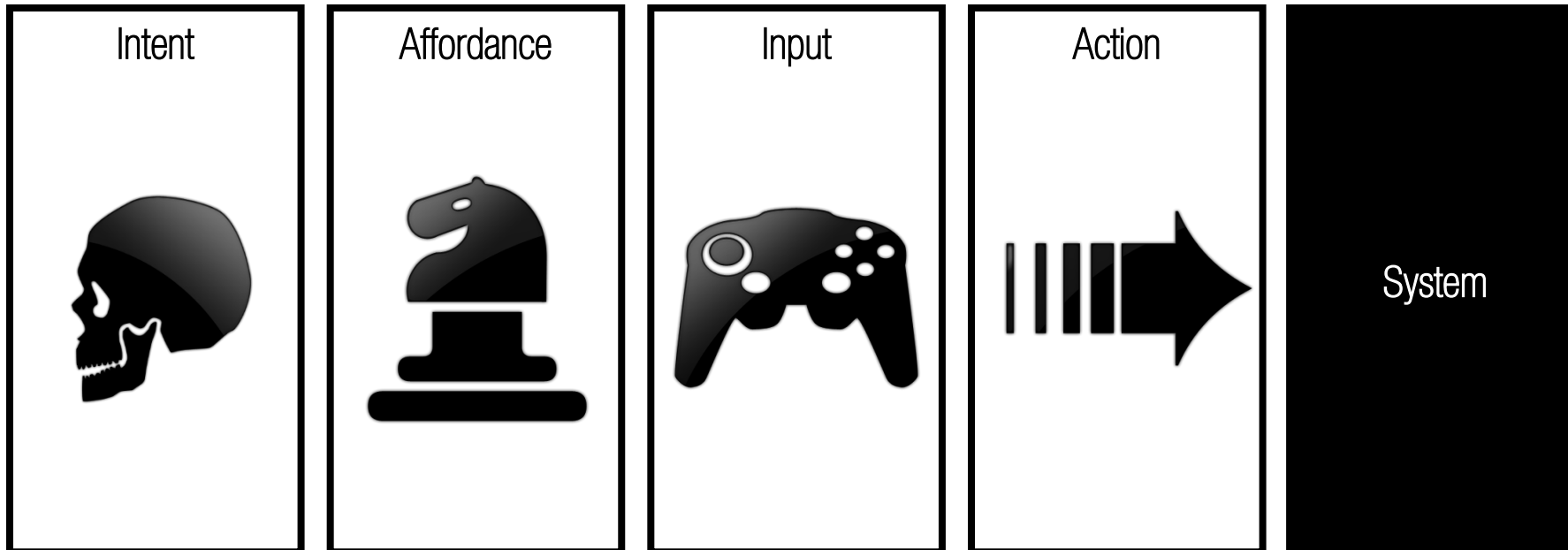
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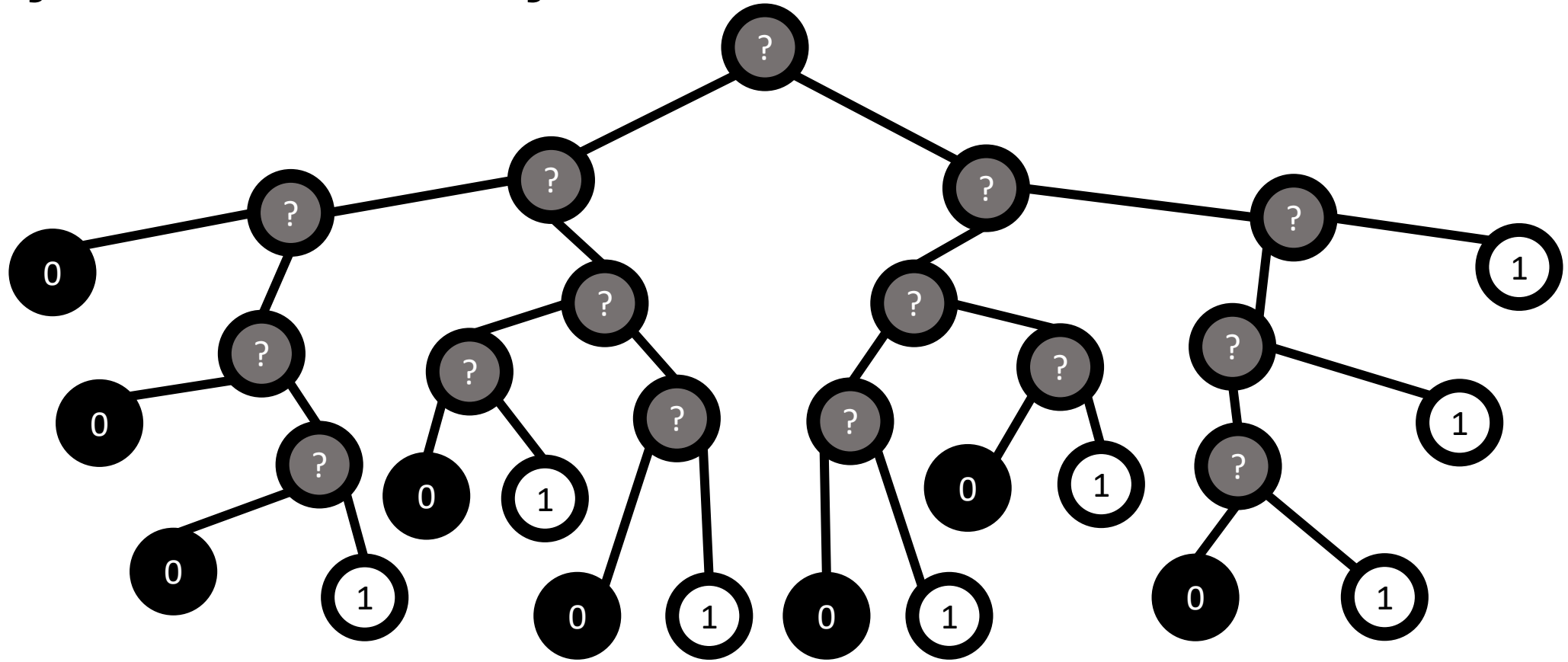


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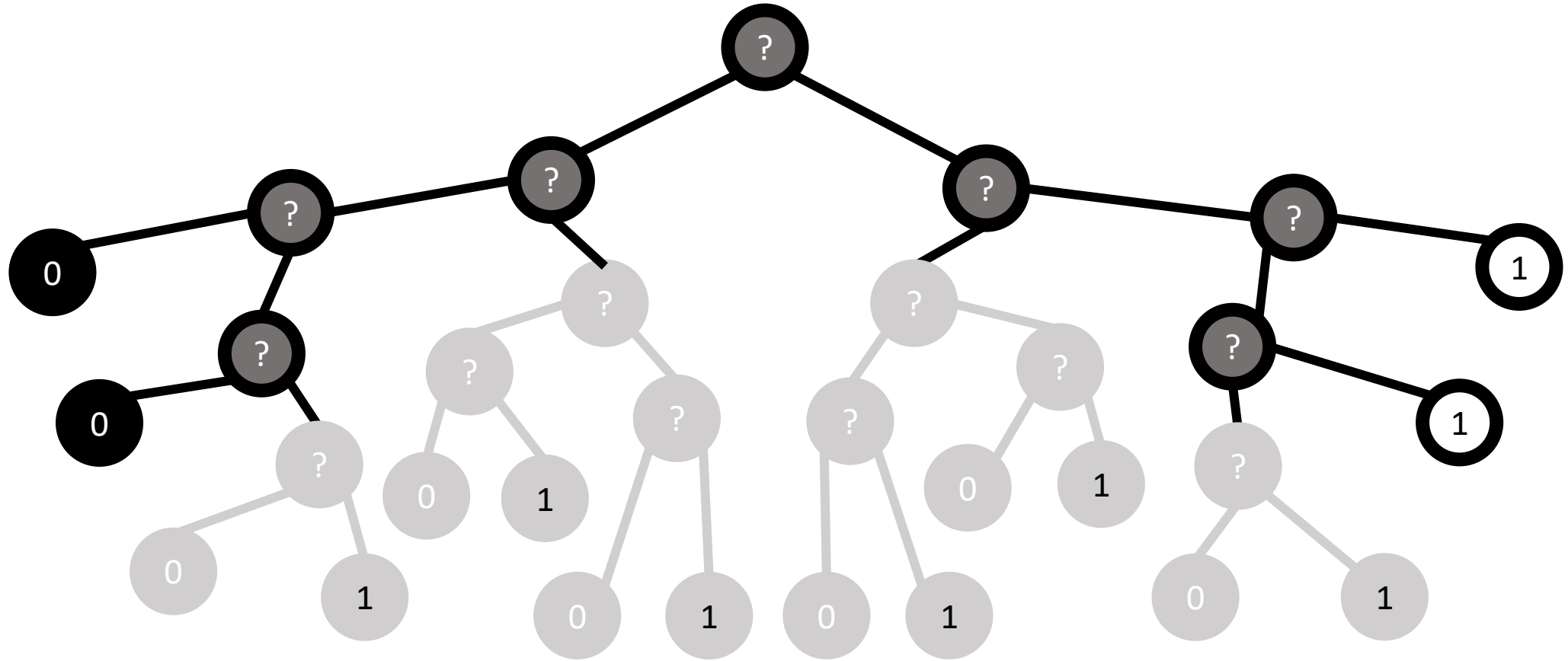
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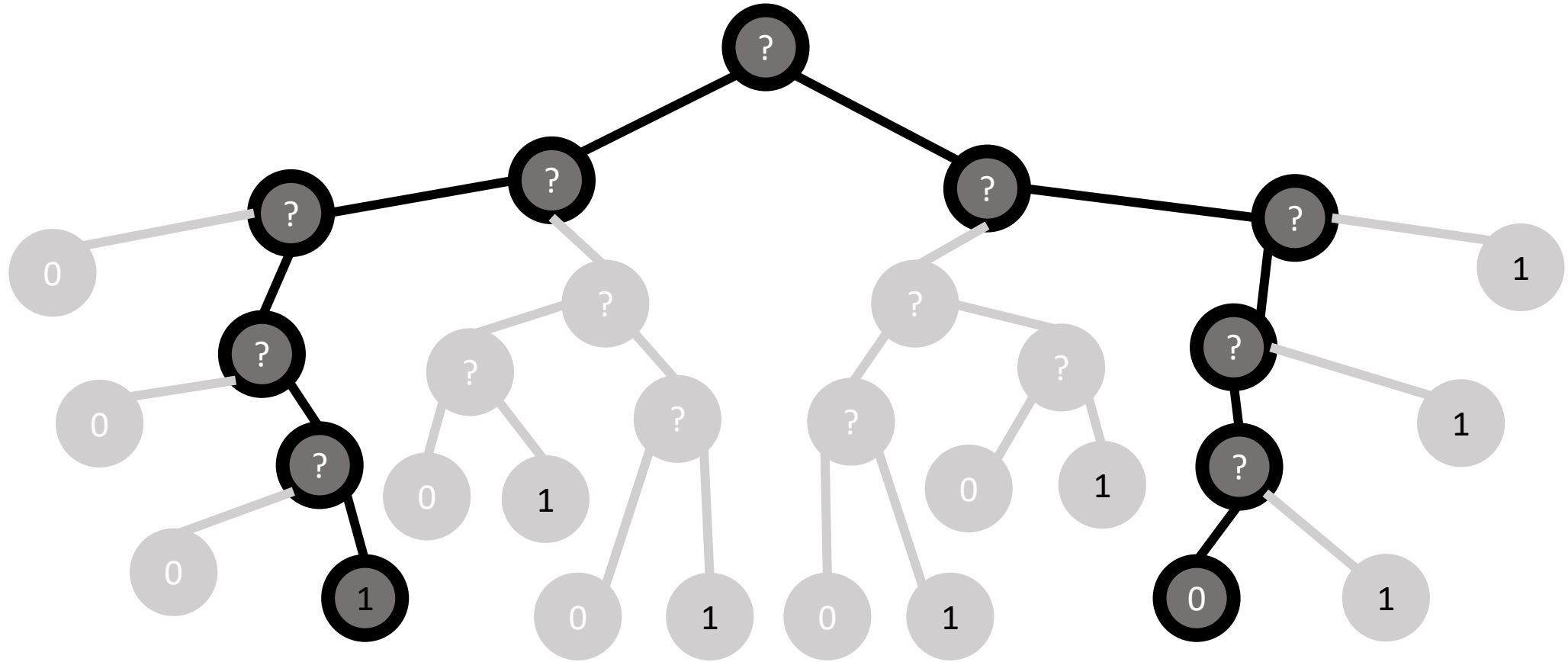
Play is indeterminacy



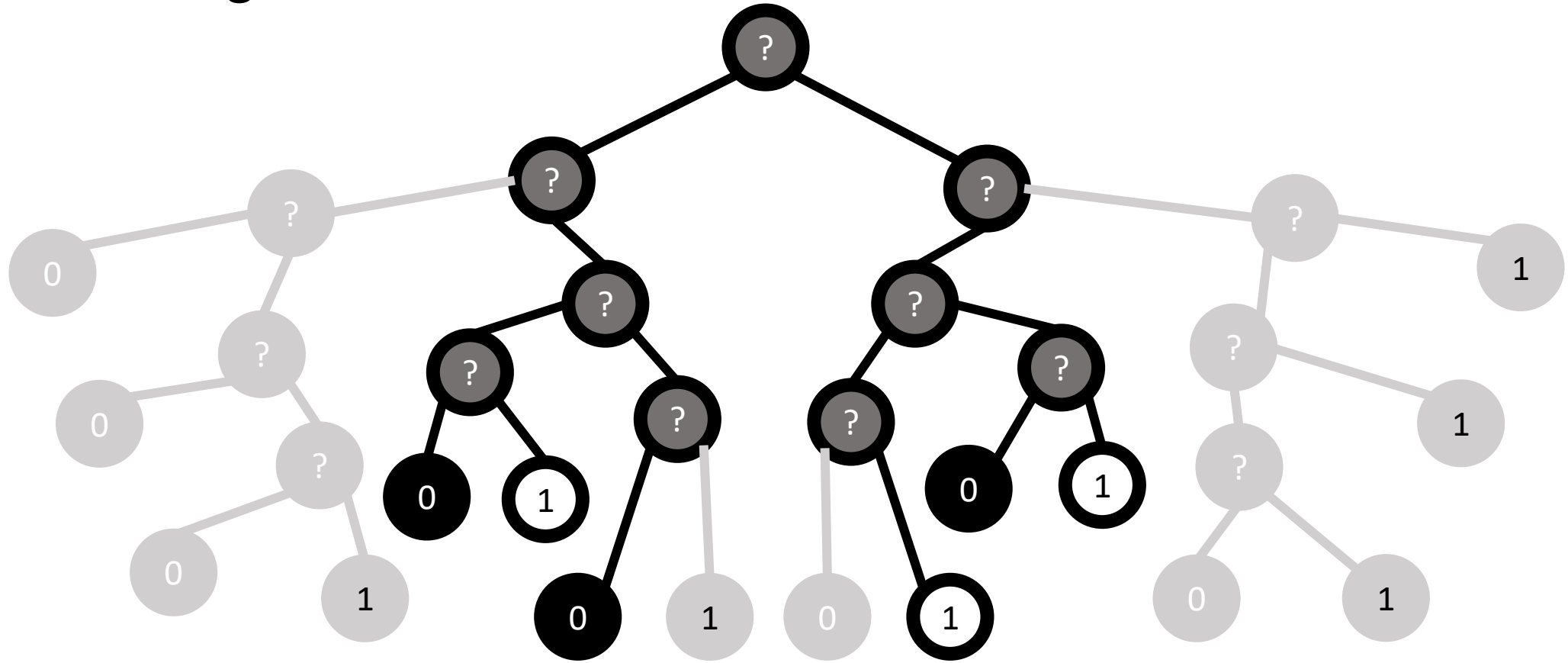
“Blow outs”



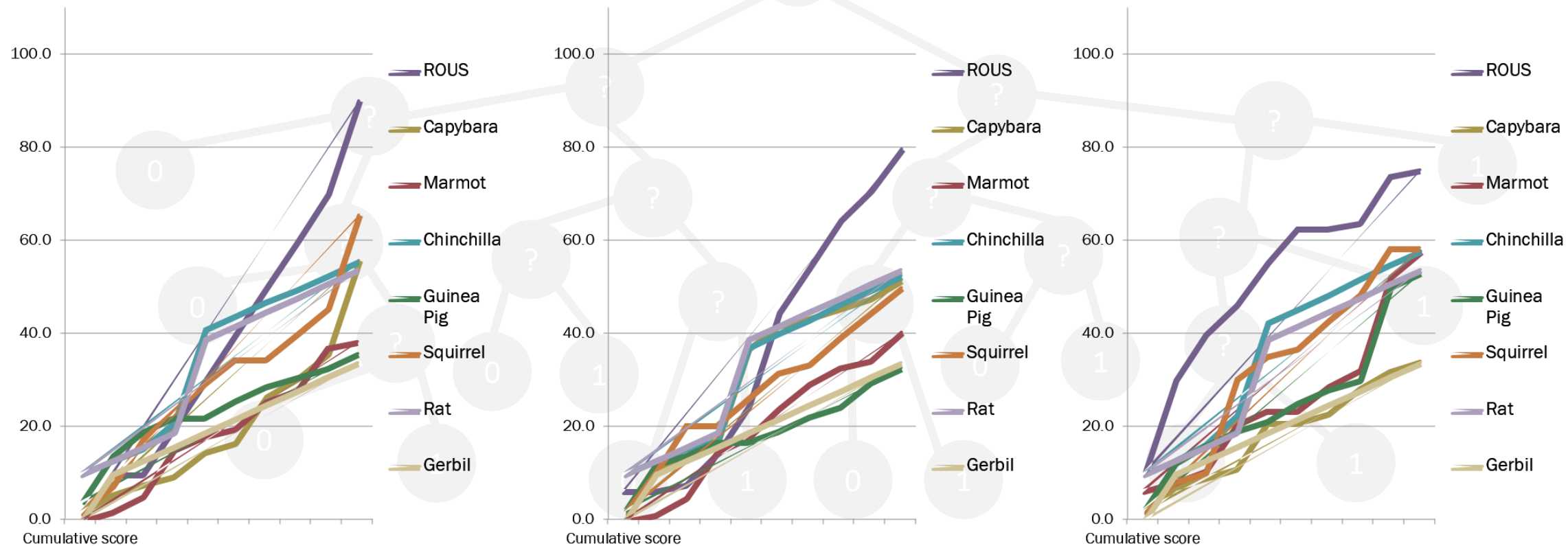
"Comebacks"



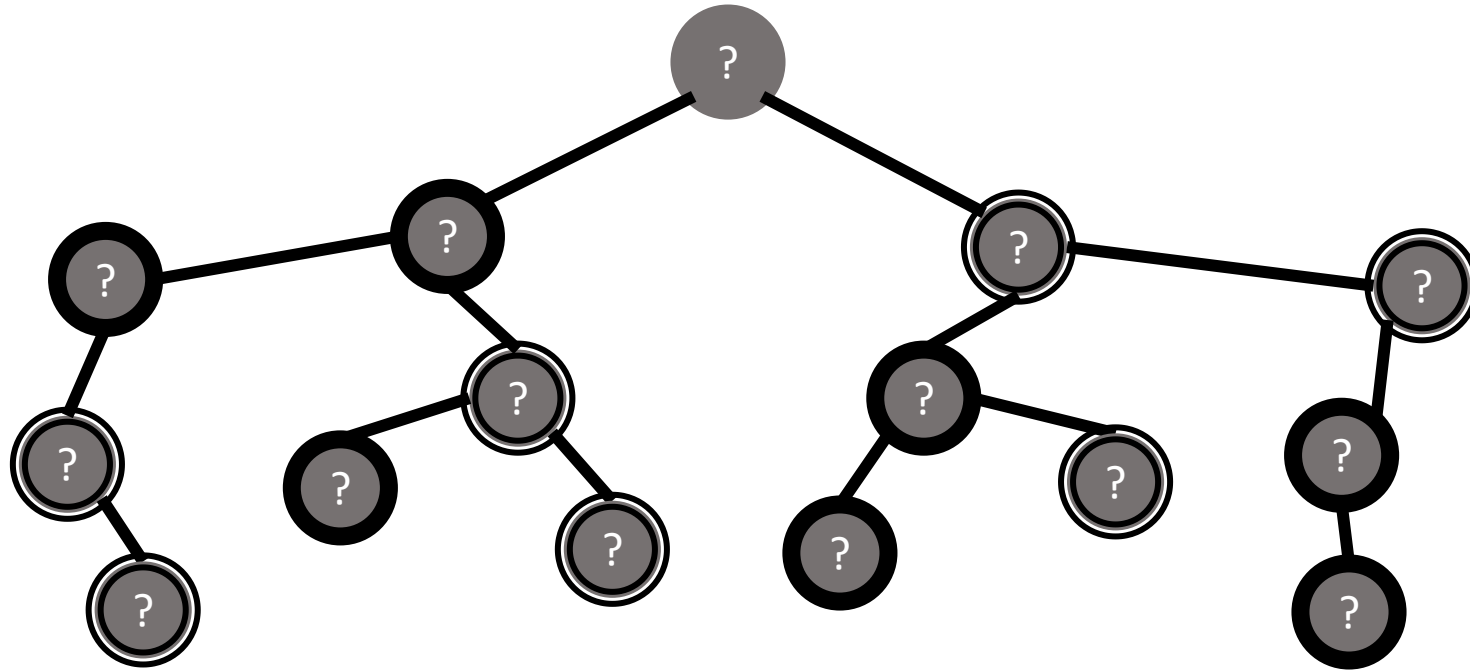
“Hard fought”



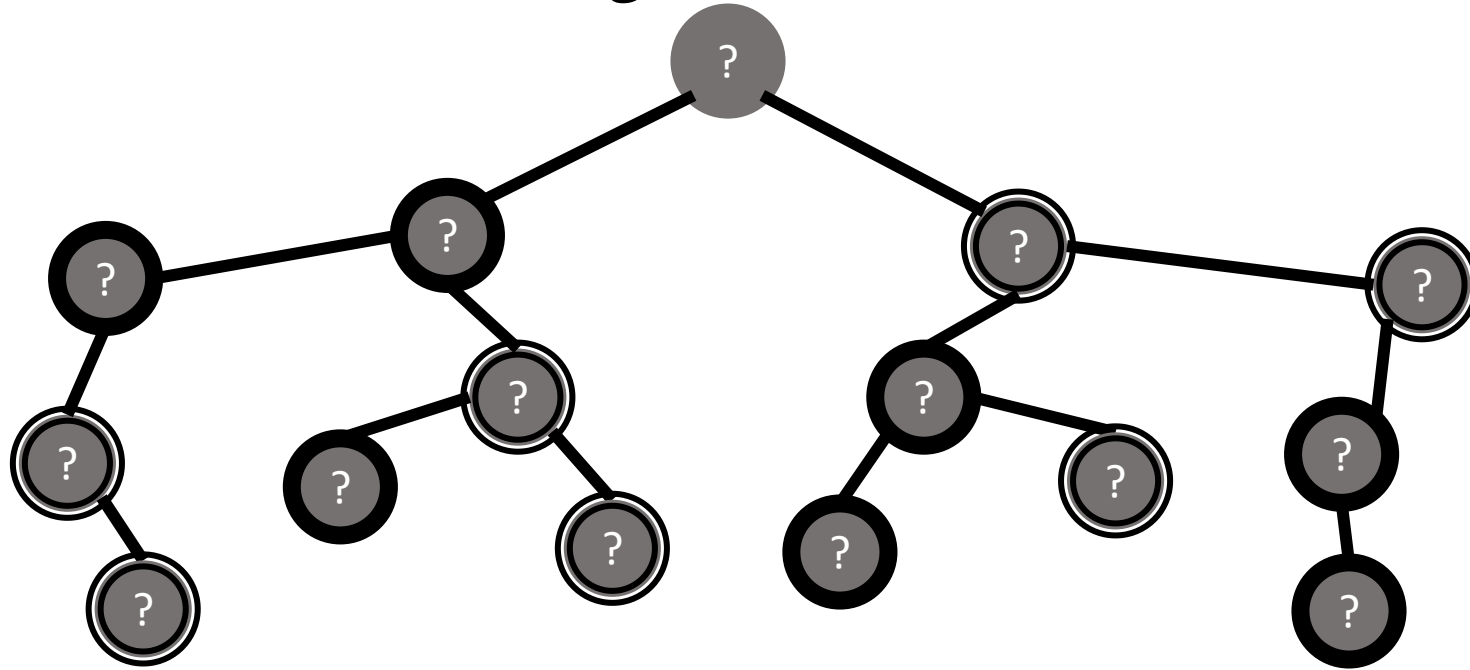
“Hard fought”



Limited look-ahead



Consider nodes as *strategies*



- A human-centric rather than computer-centric view:
 - To a human not all affordances are visible.
 - And an affordance **is also a game**.

Parity problems

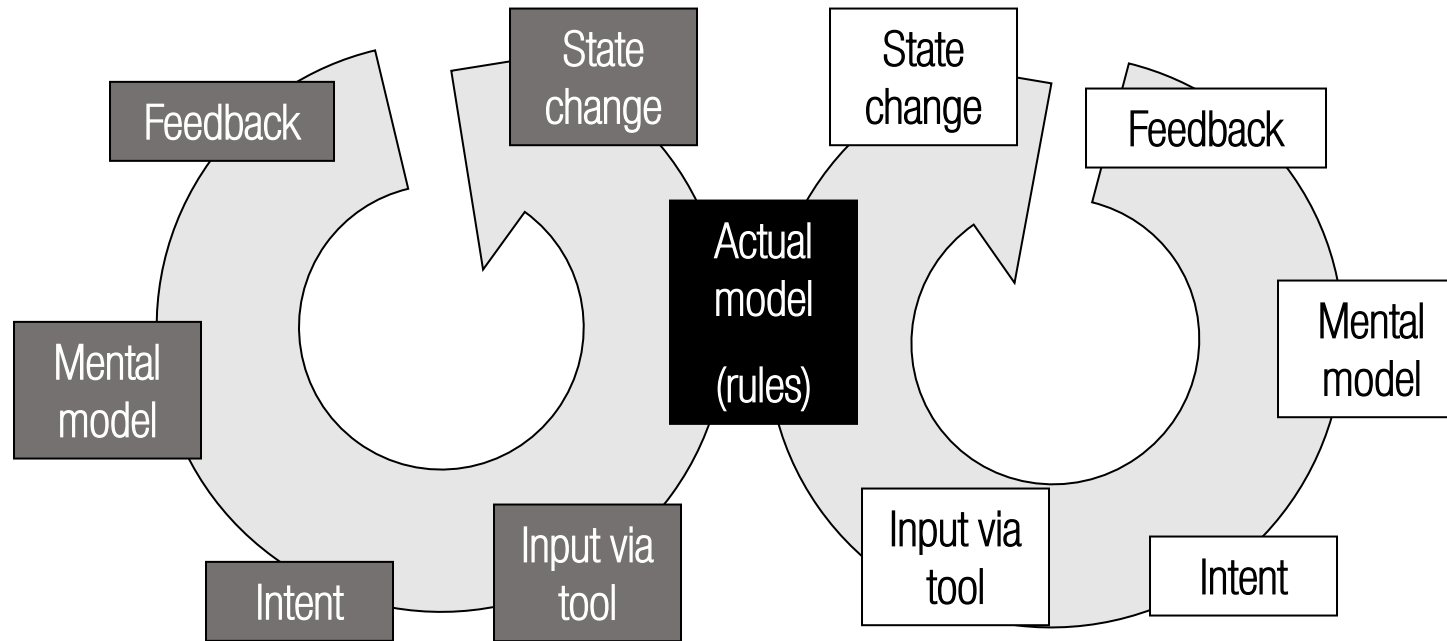
- We can think of gains and losses as we move down the tree as a parity problem.
 - In the complexity theory sense, or the permutation sense . . . not the sieve theory sense.
 - Indeed, there are games where passing (a shift-by-one) is an important strategy.
- More importantly, choice of a branch is effectively an evaluation of the total parity of the foreseeable tree.
 - Practical takeaway: orthogonal rules presenting two types of victory points instantly add depth for humans, because the two branches may favor different win conditions.

Unbounded or cyclical games

- Most games incorporate cycles in their tree.
 - Once you see the tree as loops that can run infinitely, trees start looking like an inadequate visualization or mental model.
 - Hence why systems theory tools are so popular in grammar-style approaches.
- Games where there isn't a unidirectional transfer of available resource.
 - Narratively centered games. Huge area!
 - State shifting, such as moving tokens.
 - Games where pieces can be added and removed, leading to cycles and loops.
 - Many games special case loops.
 - *Draw by threefold repetition in chess: a recursion limit.*
 - *The ko rule in go: an illegal branch.*

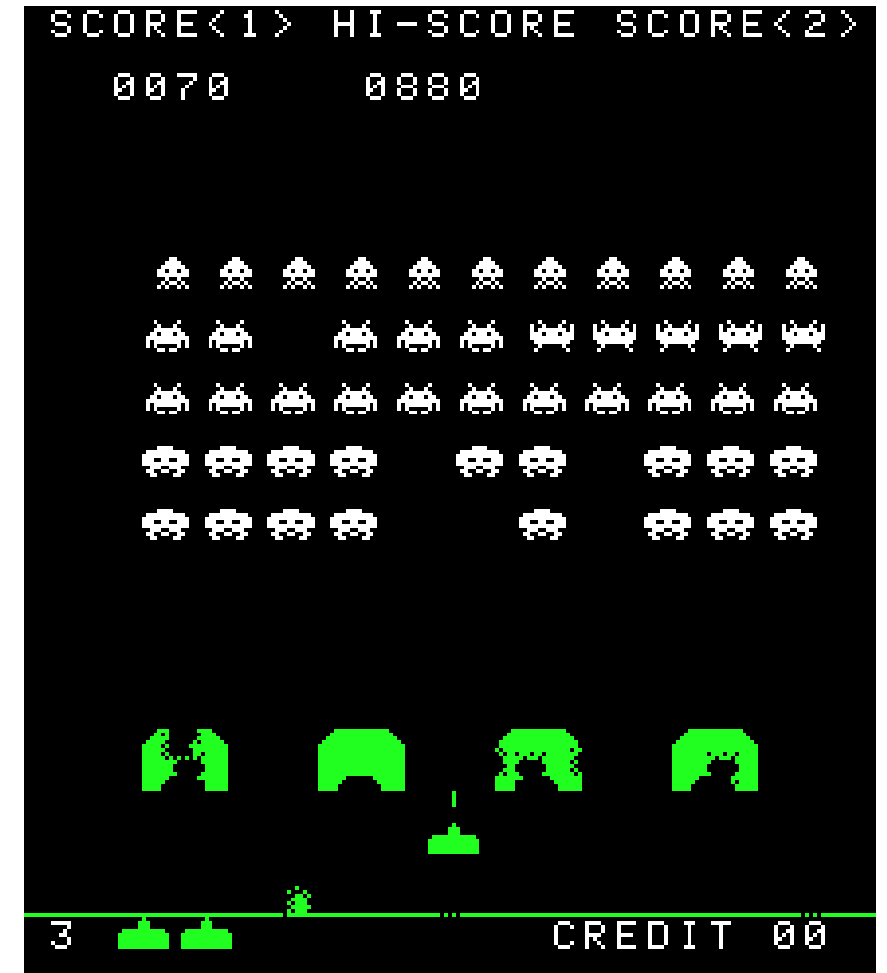
Gestures towards a BNF grammar

- game $\Rightarrow$ game + result
- result $\Rightarrow$ system(action) = (Θ , [0 , 1])



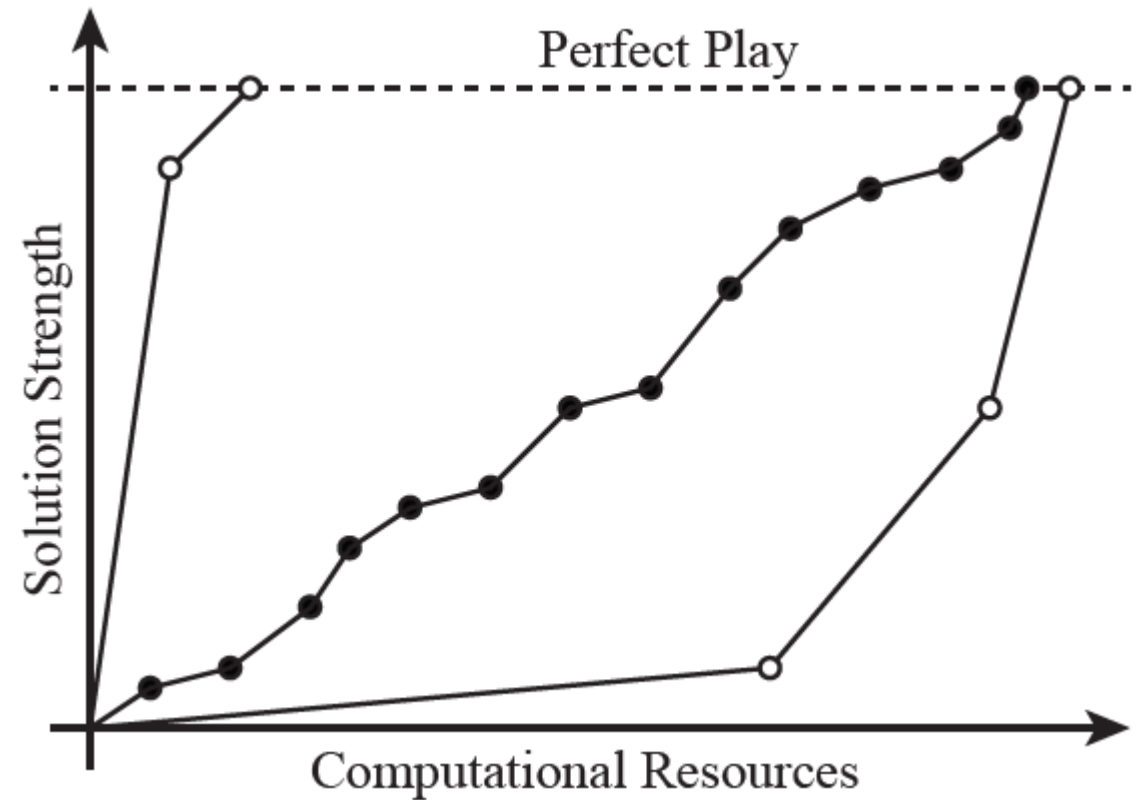
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- $\text{result} \Rightarrow \text{system}(\text{action}) = (\Theta, [0, 1])$
- $\text{system} \Rightarrow \text{side} + \text{side} \{ [, \text{side}] \}$
- $\text{side} \Rightarrow \text{player} + \text{mechanic} + \text{statistic} \{ , \text{statistic} \}$
- $\text{player} \Rightarrow ((\text{mind} + \text{experience} + \text{body}) \mid \text{AI})$
- $\text{mechanic} \Rightarrow \text{rule} \{ , \text{rule} \} + \text{statistic} \{ , \text{statistic} \}$
- $\text{rule} \Rightarrow \text{token} \{ , \text{token} \} \text{expression} \{ , \text{expression} \} \text{statistic} \{ , \text{statistic} \}$



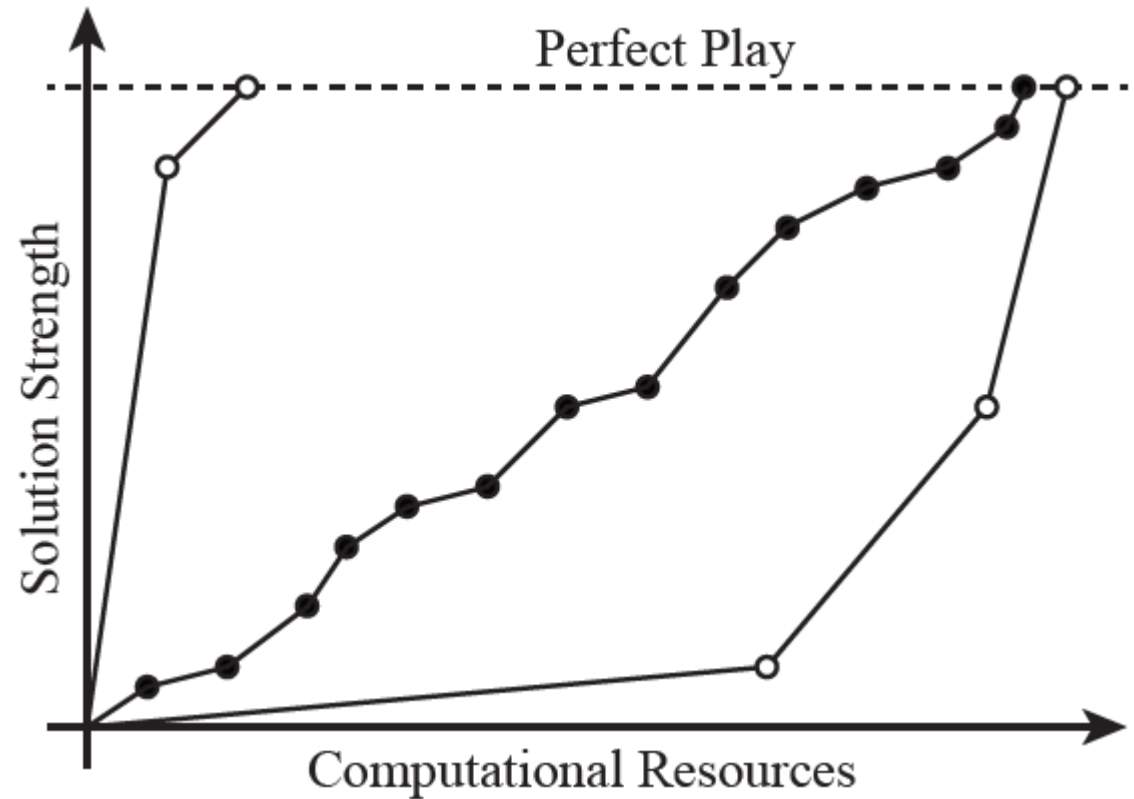
Lantz *et al*/define (a) depth: d

- The capacity for a game system to allow for a ranked population of **strategies** that provide **partial/approximate solutions**.
- The more discrete ranks in such a population, the greater the degree of this property within the game.



Implications

- A quality of the number of intermediate strategies, or **heuristics** short of optimality, that a player can discover as they proceed to complete mastery.
- A game you can play optimally or near optimally with **a computationally cheap strategy** lacks $\mathcal{d}$.
- A game you can't discover new strategies in will also lack $\mathcal{d}$ because it's based on skill chaining or learning. In a sense, depth by their criteria is based on lemmas, on plateaus.



Heuristics = strategies

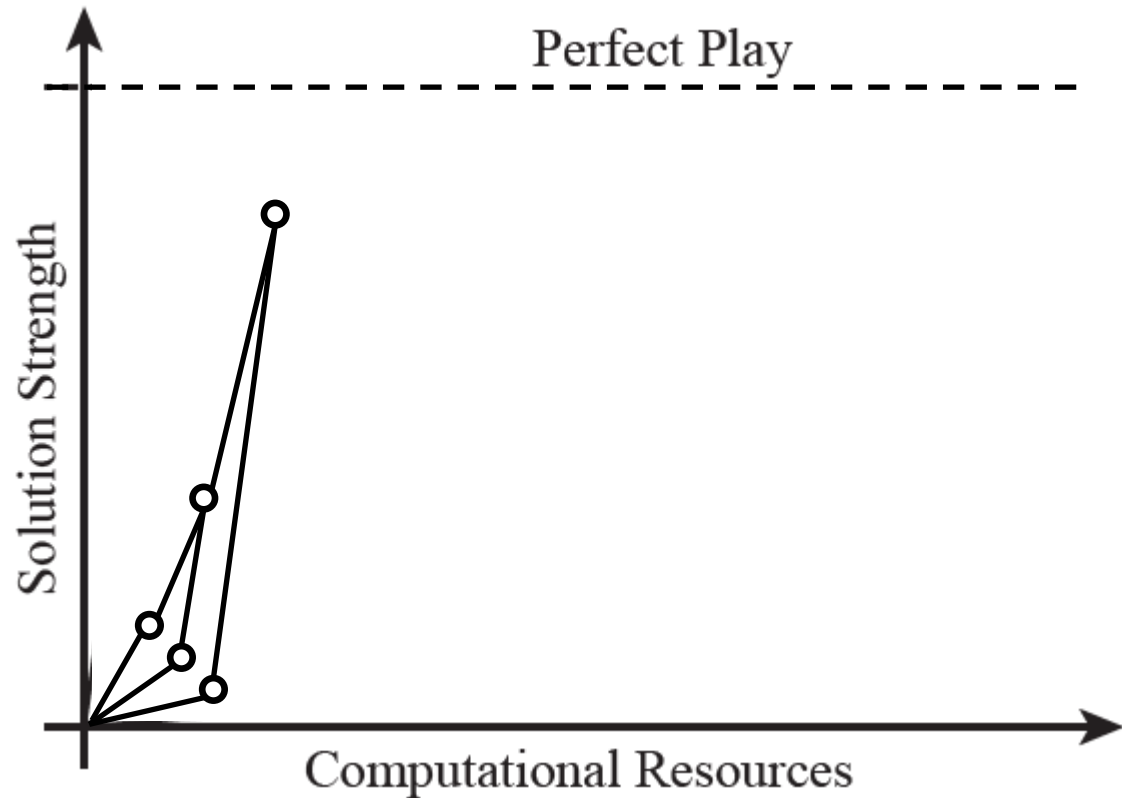
- “Control the center” $\Rightarrow$ stay in this area of the state space.
- Regularity in the tree bounds the “good game” space.
 - Too high means degenerate strategy; it's easy to arrive at optimal play.
 - Too low means no heuristics work, because of excessive variability.
- Heuristics are effectively brute force search shortcuts in this view.

Flaws as utility function for designers

- **Heuristic abandonment isn't represented.**
 - A classic form of learning is to reach a lemma and be obliged to abandon previous mental models.
- **Non-transitive strategies aren't accounted for.**
 - Rock-paper-scissors structures at the low end, rich structures in fighting games.
- **We don't have any good way to measure computational complexity per heuristic.**
 - And if we solve the game, all heuristics but one are retroactively disproven.
- **The Dan Cook critique:** “Any rubric for depth that does not include a psychological filter will always result in examples that are interesting for a machine, but uninteresting to a human.”

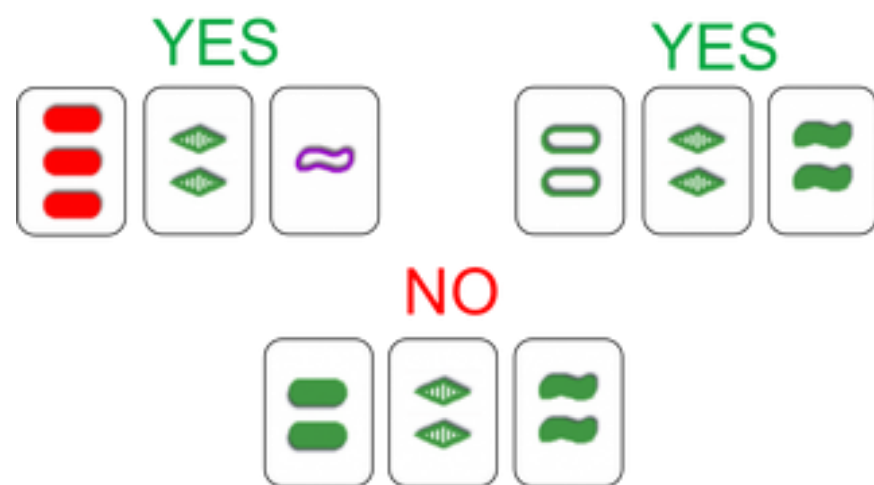
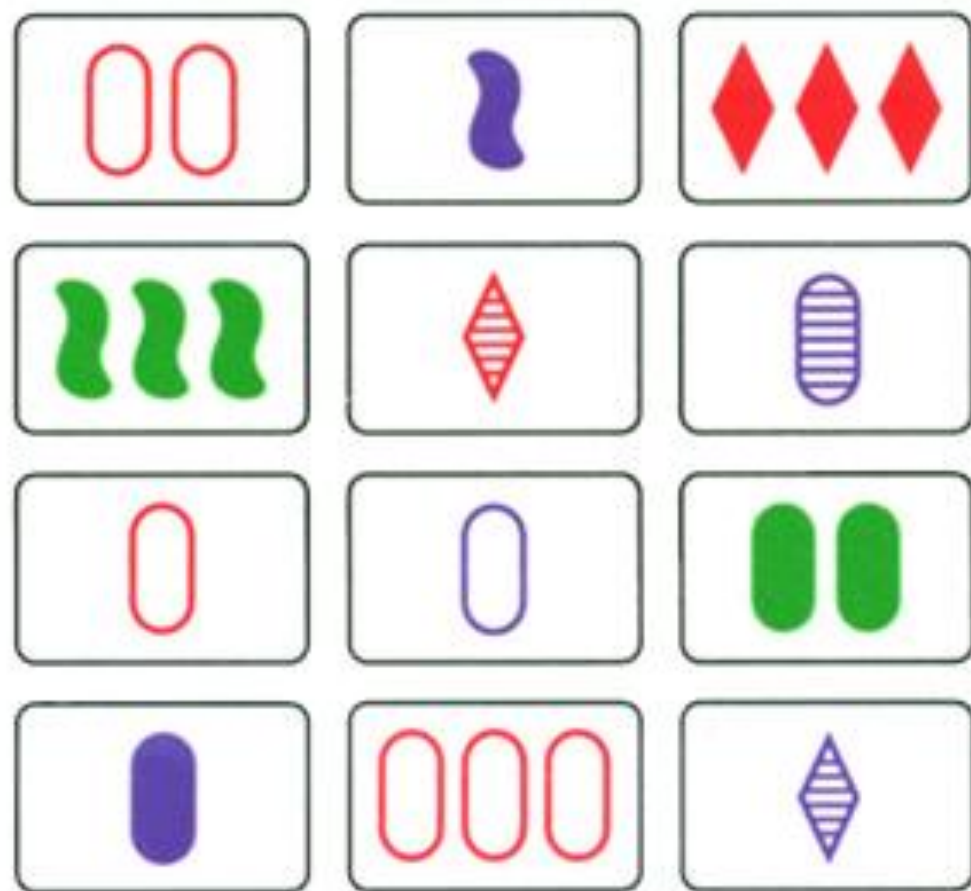
What about this game?

- The game offers many heuristics...
 - All of roughly the same strength.
 - All of roughly the same computational resources.
- Rather than heuristics chaining, higher solution strength is achieved by heuristic **selection and combination**.
 - And a lot of this is about **affordances** not inherent complexity.



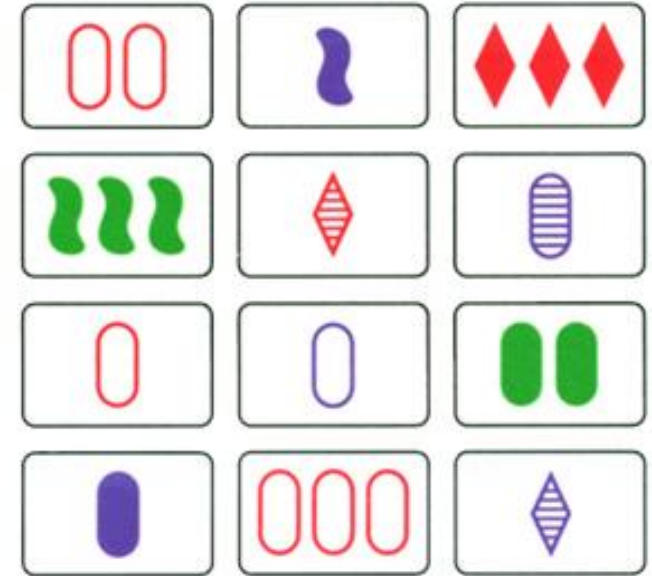
Example: Set





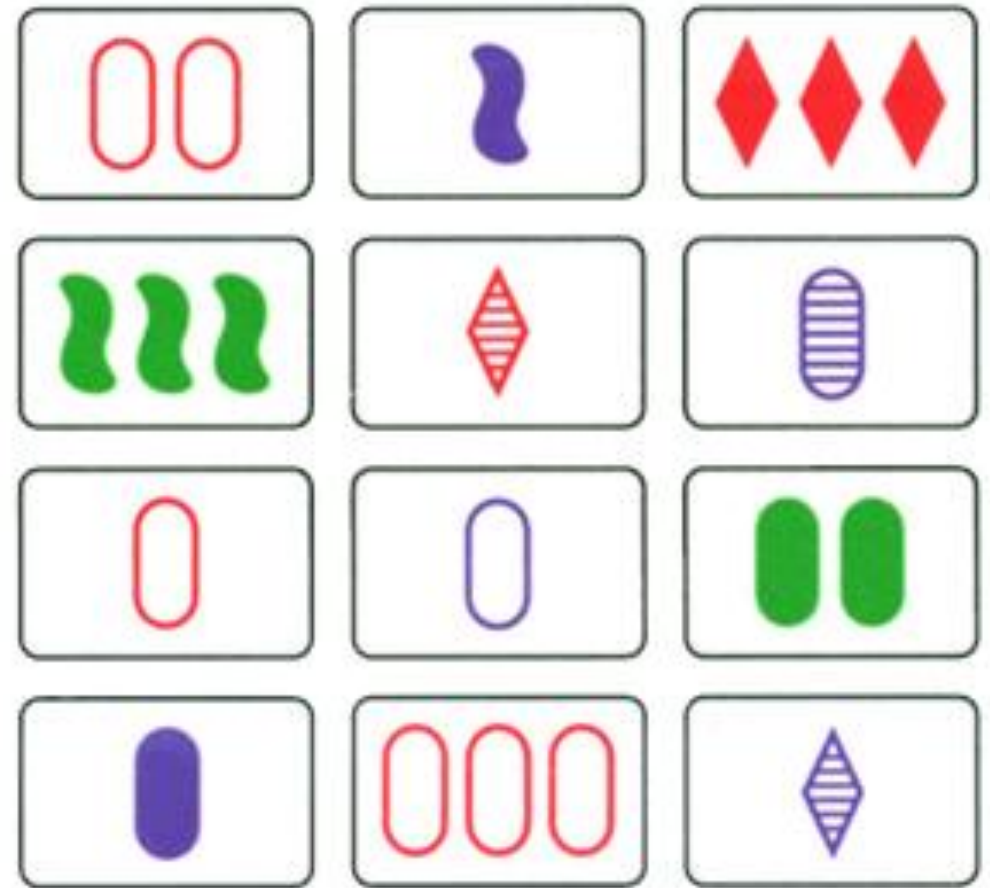
Computer algorithm

- Equal capability to group things, given image recognition or data.
 - No preference in algorithm, except the ordering of IF statements.
 - 12 card spread is trivial; can brute search everything.
-
- **Strategy vs equal competitor would be about choosing IF statement ordering.**
 - Select an algorithm that reduces the available sets that opponents search for first, so that computation speed increases over iterations.
 - E.g., if all computers search color first, the computer that searches for sets that tend to reduce color commonality sets would gradually come out ahead.
 - But a computer that selects search method randomly wouldn't be vulnerable to this attack.



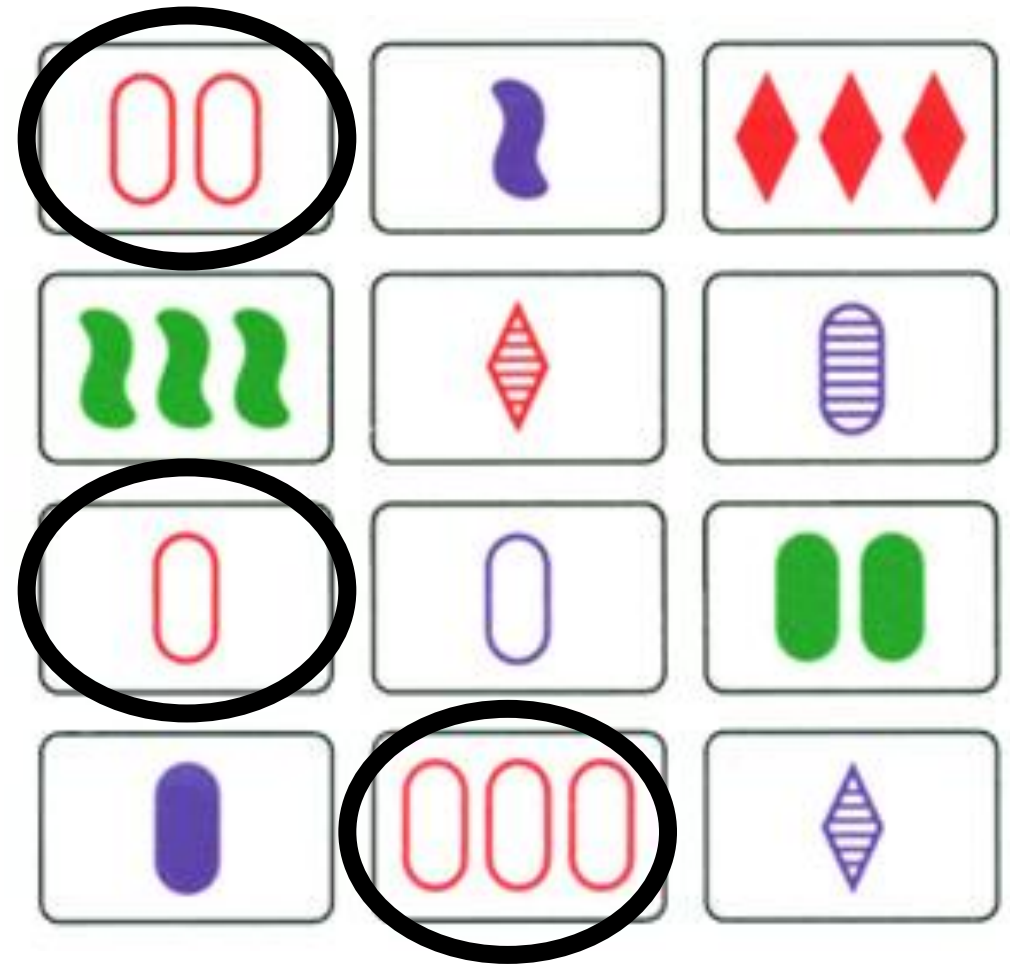
Human strategies

- Humans find some types of congruency easier to see.
 - All the same on any axis is the easiest to match.
 - Next easiest is quantity sequence.
 - Then come shape and shading.
- Human cognition clusters, rather than run brute force search.
 - A player who focuses on shape difference sets first may disrupt other players by destroying viable sets remaining in the deck.



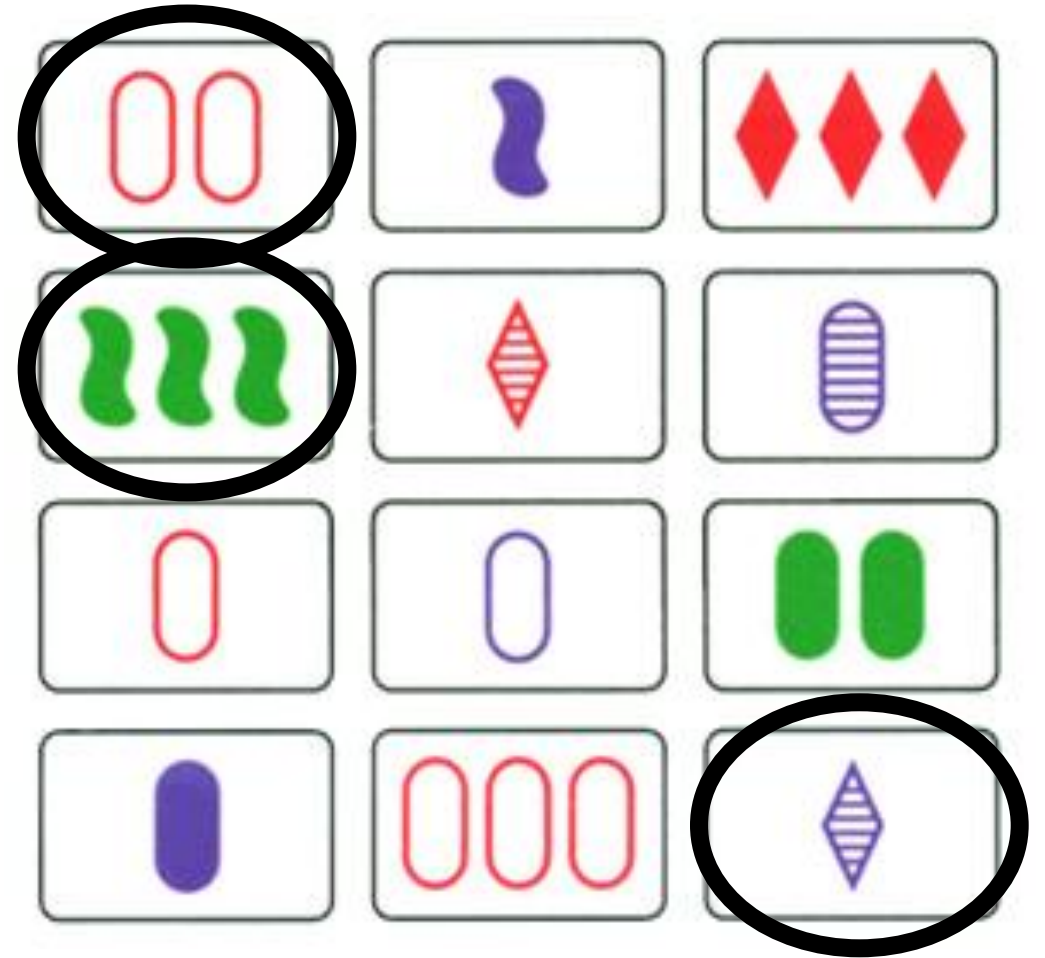
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 - E.g. a player who searches non-congruity first prefers high entropy spreads.



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Forms of indeterminacy affect computational resources

- **Input randomness:** where the landscape for the system is randomized.
 - Forces use of heuristic selection; lots of possible x 's for $f(x)$.
- **Output randomness:** where a system result is randomized rather than simulated.
 - Forces contingency planning.
- **Hidden information:** where a portion of the critical data for a decision isn't available and has a wide spread of possible values.
 - Increases raw search.
- **Practical non-computability:** where perception time, reaction time, and execution time are all so tight that you can't actually use anything other than instinct and reflex.
 - Analogizes to computational complexity, but admits of the human.

Is depth about...

- ...the actual complexity of the game?
 - Systems that are NP-Hard, and so on.
- ...the ability to learn more ways to approach the game?
 - If so, we can't leave out "how the player learns these."
- ...building mental models of the opponent's mental model?
 - "Yomi" (cf David Sirlin, fighting game community)
 - For that matter, what about mental models of **teammates**?

Alternative takes on depth

- A count of iterations where parity is not expressible as Θ or 1 and the parent wasn't also indeterminate.
 - This would capture high complexity systems, eliminate trivial branching, and also capture other forms of indeterminacy.
- The number of hidden affordances (e.g., possible actions)
 - A measure of the complexity level for **perceiving** each affordance.
- The number of possible intents a player could possibly have.
 - Which isn't in any way measurable, but is driven by systemic properties (inputs, etc).

Moment #37

- Daigo is down to one pixel of health. His opponent has plenty left.



<https://www.youtube.com/watch?v=KS7hkwbKmBM>

Was this deep?

What are the design takeaways?

Moment #37

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 - A super attack that involves fifteen separate blows, any one of which would be fatal.



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- He then executes fifteen perfect parries, again with 7ms accuracy **each**.



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- He also anticipates when it will begin to within 7ms accuracy.
- He then executes fifteen perfect parries, again with 7ms accuracy **each**.
- And then executes his own super attack. And wins.



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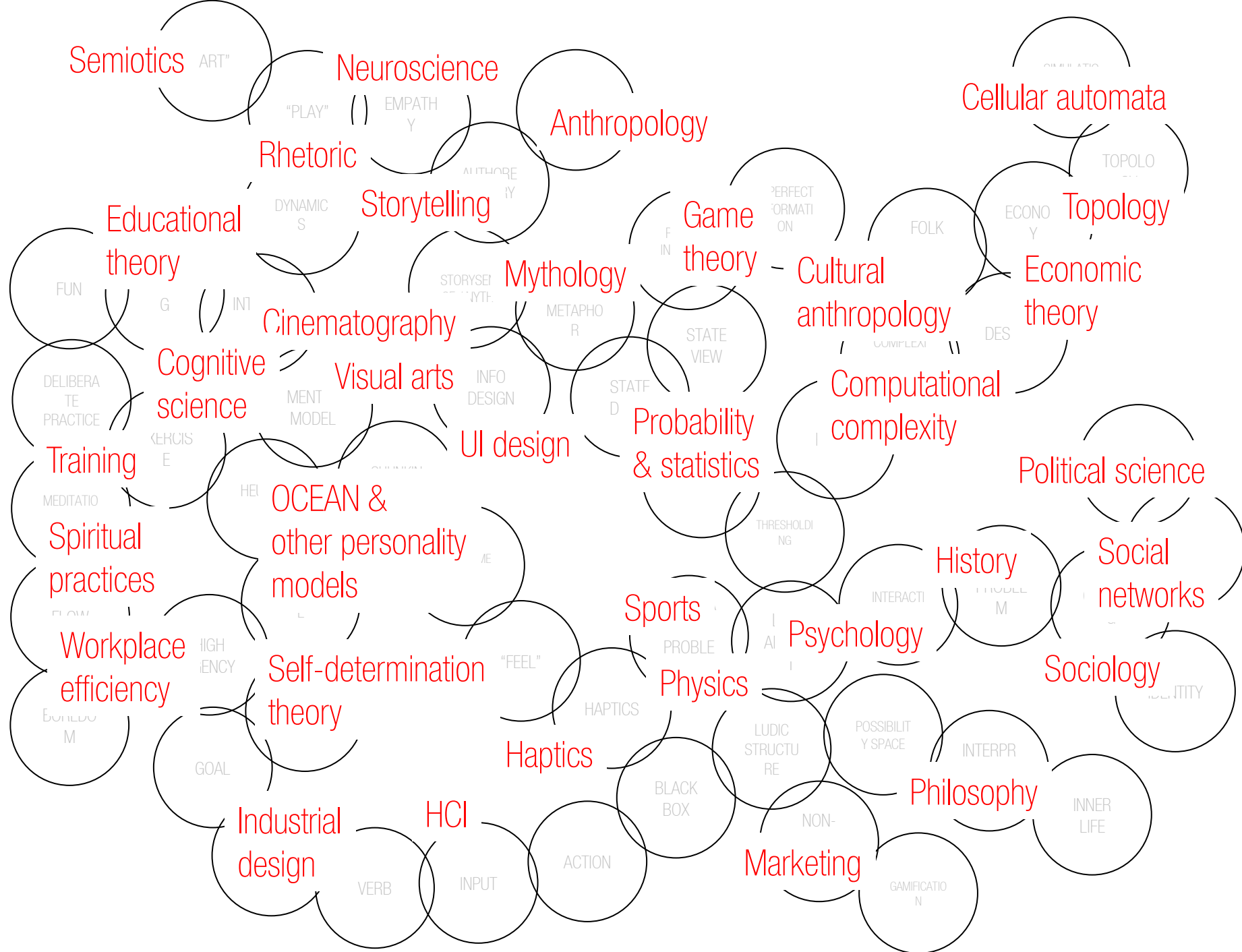
The grammar doesn't say

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- $\text{rule} \Rightarrow \text{token} \{ , \text{token} \} \text{expression} \{ , \text{expression} \} \text{statistic} \{ , \text{statistic} \}$
- $\text{action} \Rightarrow \text{verb} [\{ + \text{action} \}] (\text{data})$
- $\text{verb} \Rightarrow \text{intent} + \text{input}$
- $\text{input} \Rightarrow \text{affordance} + \text{action} [+ \text{game}]$
- $\text{affordance} \Rightarrow \text{player} (\text{data})$

But it's probably ALL of these:

- System of sufficient complexity to permit emergence, nonlinearity, etc.
- Non-transitive strategies.
- Unfolding of heuristics, and heuristic abandonment too.
- Affordances and perceptual limits.
- Yomi, modeling opponent mental models.





Thank you!

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